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## *Keynote*

# **Milestones in altimeter performance: Past, Present, and Future** *with relevance to Coastal Altimetry*

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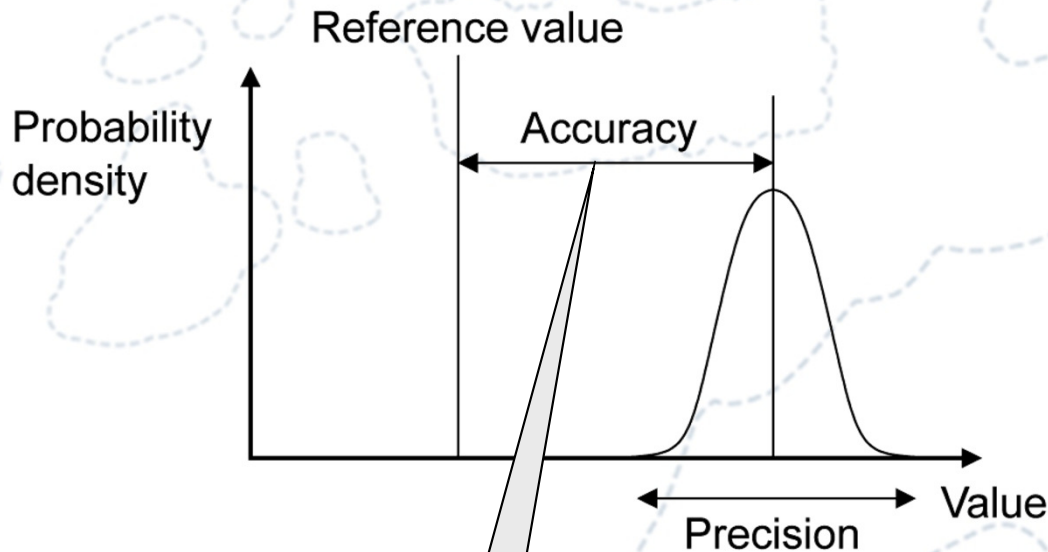
## Outline

- Foundations
- The “conventional” altimeter
- Delay-Doppler
- Maximizing (SSH) precision
- Further possibilities
- Conclusions





# Accuracy vs Precision



*ACCURACY*  
and  
*PRECISION*  
two common terms;  
emphasis here is on  
Precision

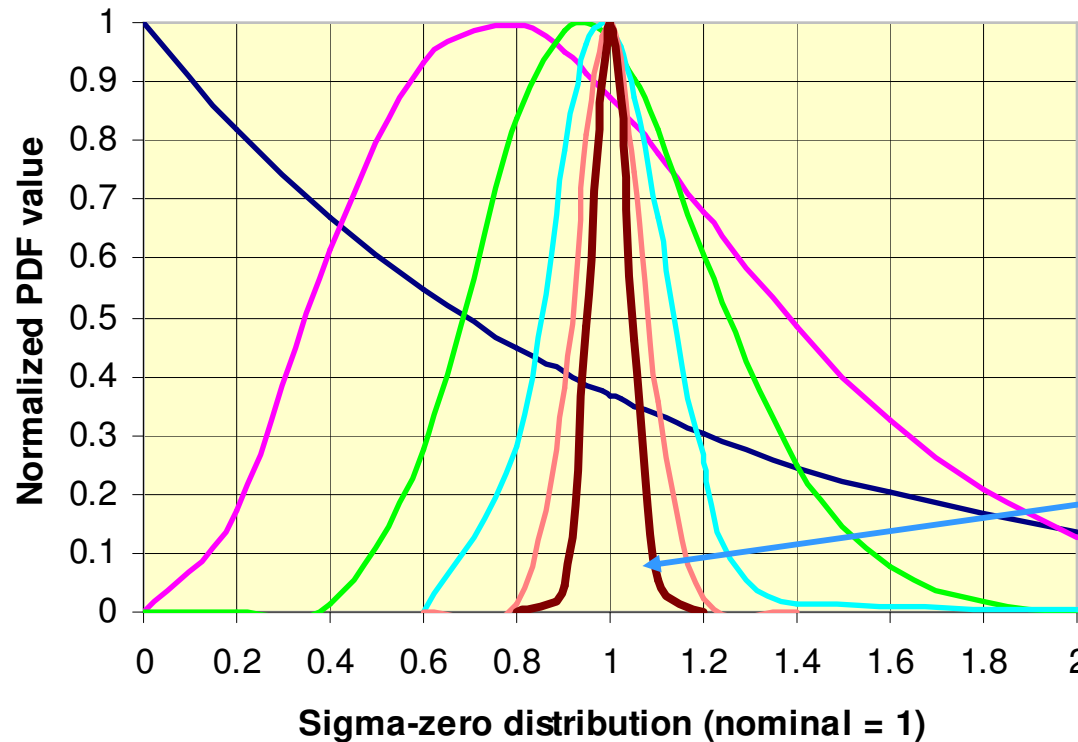
Logical  
synonyms

Mean  
"Average"

Standard deviation  
Variance (STD<sup>2</sup>)

# On Precision (*wrt* Radar Self-Noise)

Gamma Distribution as a function of N  
(mean and peak normalized)



All radars are "precision-challenged" =>  
"maximize averaging"!

- N = 1 (Single-look SAR)
- N = 4 (Typical SAR image)
- N = 16 (Mini-RF Lunar SAR)
- N = 64 (WS scatterometer)
- N = 200 (Radar ALT @ 10 Hz)
- N = 600 (DDA @ 10 Hz)

*N* is the number of statistically-independent samples averaged for a given measurement



# The “conventional” altimeter

**1973: Skylab**

Short pulse: proof of concept altimeter

**1975: GEOS-3**

LFM pulse; “Brown model”, pulse-limited footprint

**1978: Seasat**

Full de-ramp (long linear fm pulse), *also known as “stretch”*

**1985 – “recently”:** *Same basic approach: “LRM”*

**Geosat; GFO**

**ERS-1, -2; Envisat**

**Topex/Poseidon; Jason-1, 2**

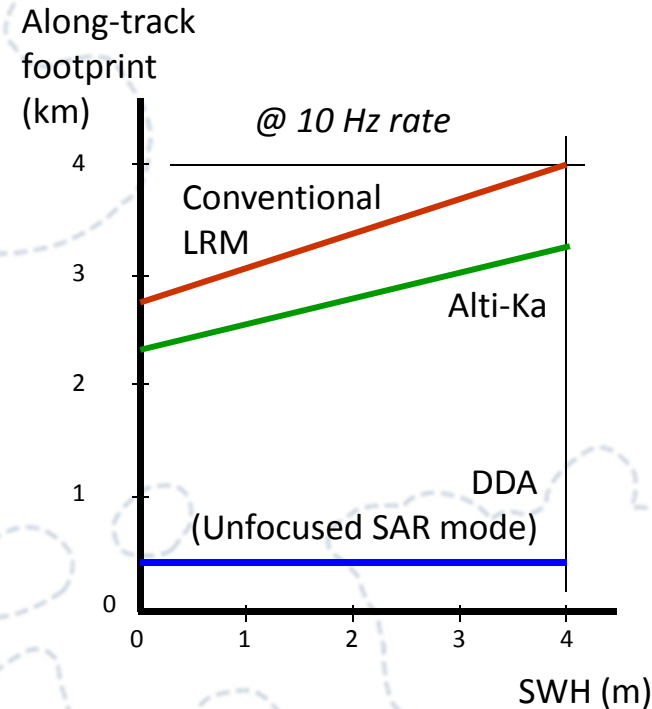
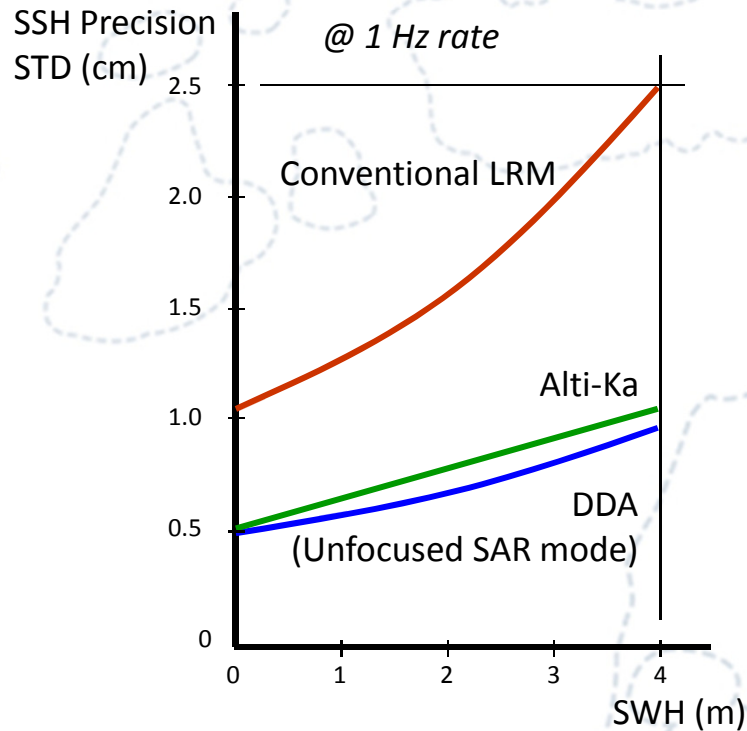
**Alti-Ka (LRM, but wider BW, shorter wavelength)**

---

*Green underbars denote milestones*



# Precision and (*along-track*) Footprint



From simulations, courtesy  
CNES and JHU/APL

$$X_{LRM} \approx \left( 1 + \frac{4}{7} SWH \right) D_{PL} + 7 t_P$$

$$X_{Dop} \approx 7 t_P$$

where  $t_P = \frac{1}{\text{posting rate in Hz}}$





# Delay-Doppler Altimeter

**2005:** (CryoSat-1 => “*CryoSat paradigm*” *DDA*)

**2010:** CryoSat-2

Full de-ramp

Footprint: Doppler beam-limited (along-track)

Pulse-limited (across-track)

Closed burst

Multi-mode

**(201x):** Sentinel-3

The CryoSat paradigm (“SAR mode”, no interferometer)

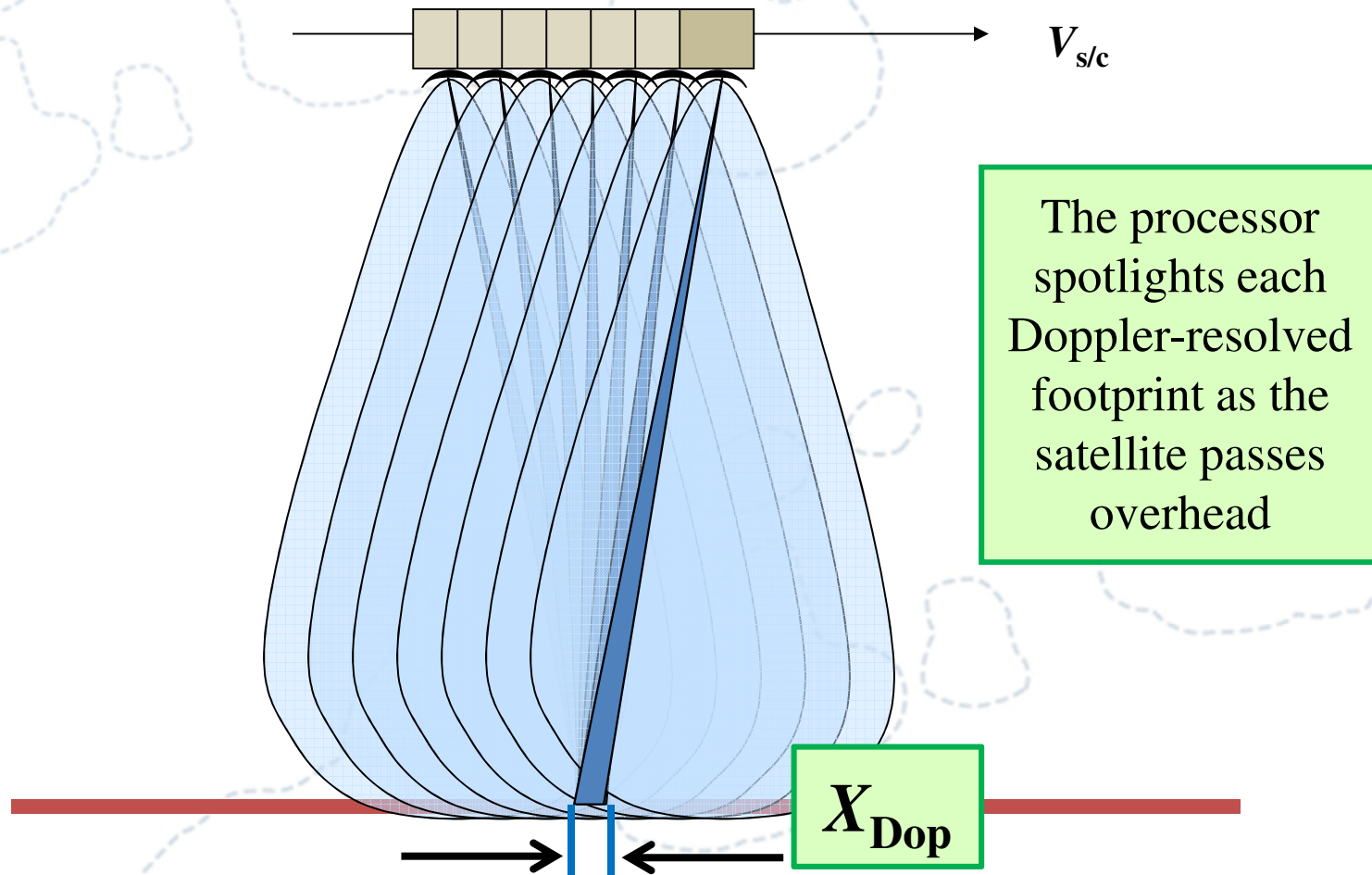
or LRM





# The Delay-Doppler Mode

*(in effect, parallel along-track beam-limited altimeters !)*



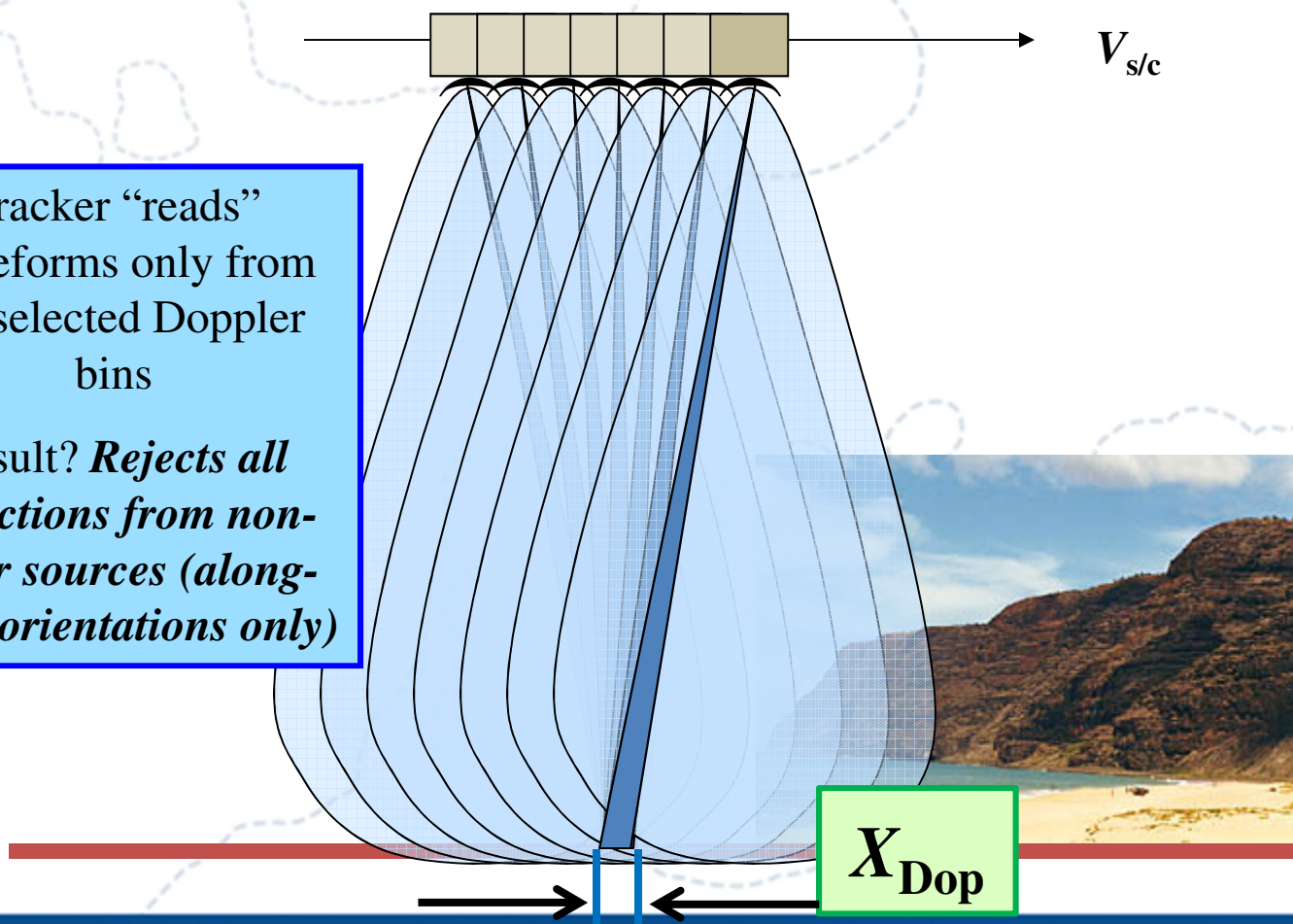


# DDA – Coastal approach/retreat

*(takes advantage of narrow beam-limited coverage)*

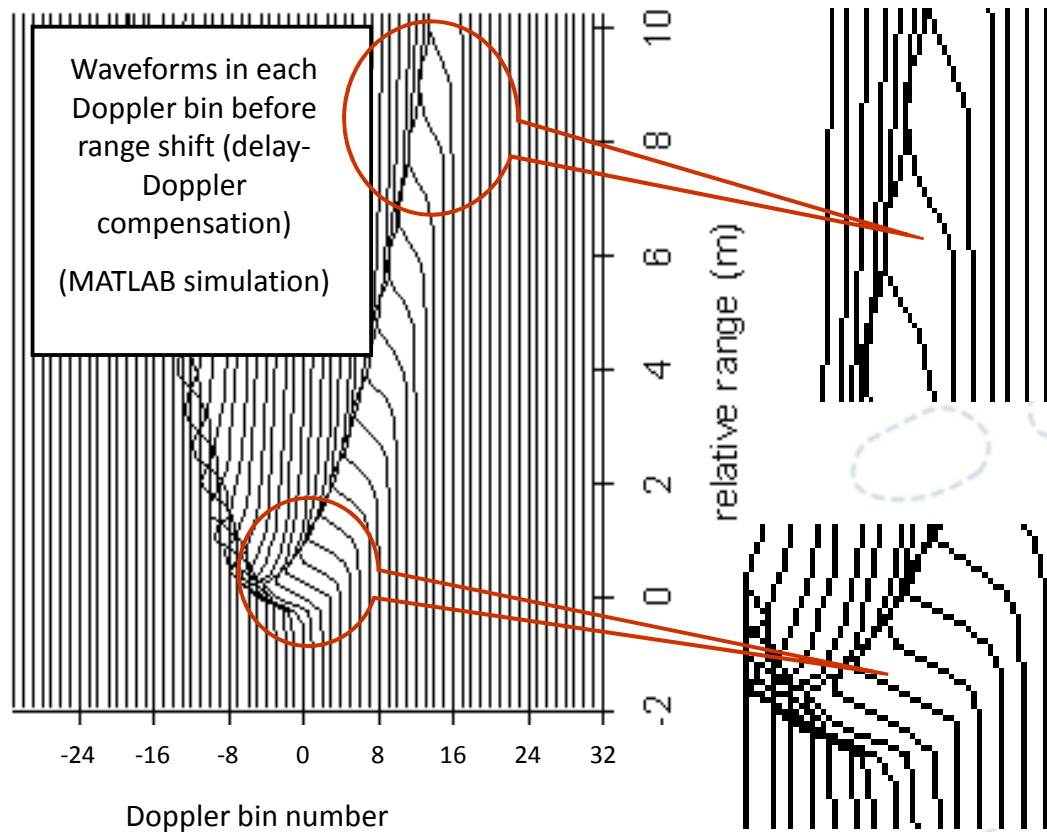
Tracker “reads” waveforms only from the selected Doppler bins

Result? *Rejects all reflections from non-nadir sources (along-track orientations only)*



# Useful Doppler bins

*(diminishing returns for larger off-nadir angle)*

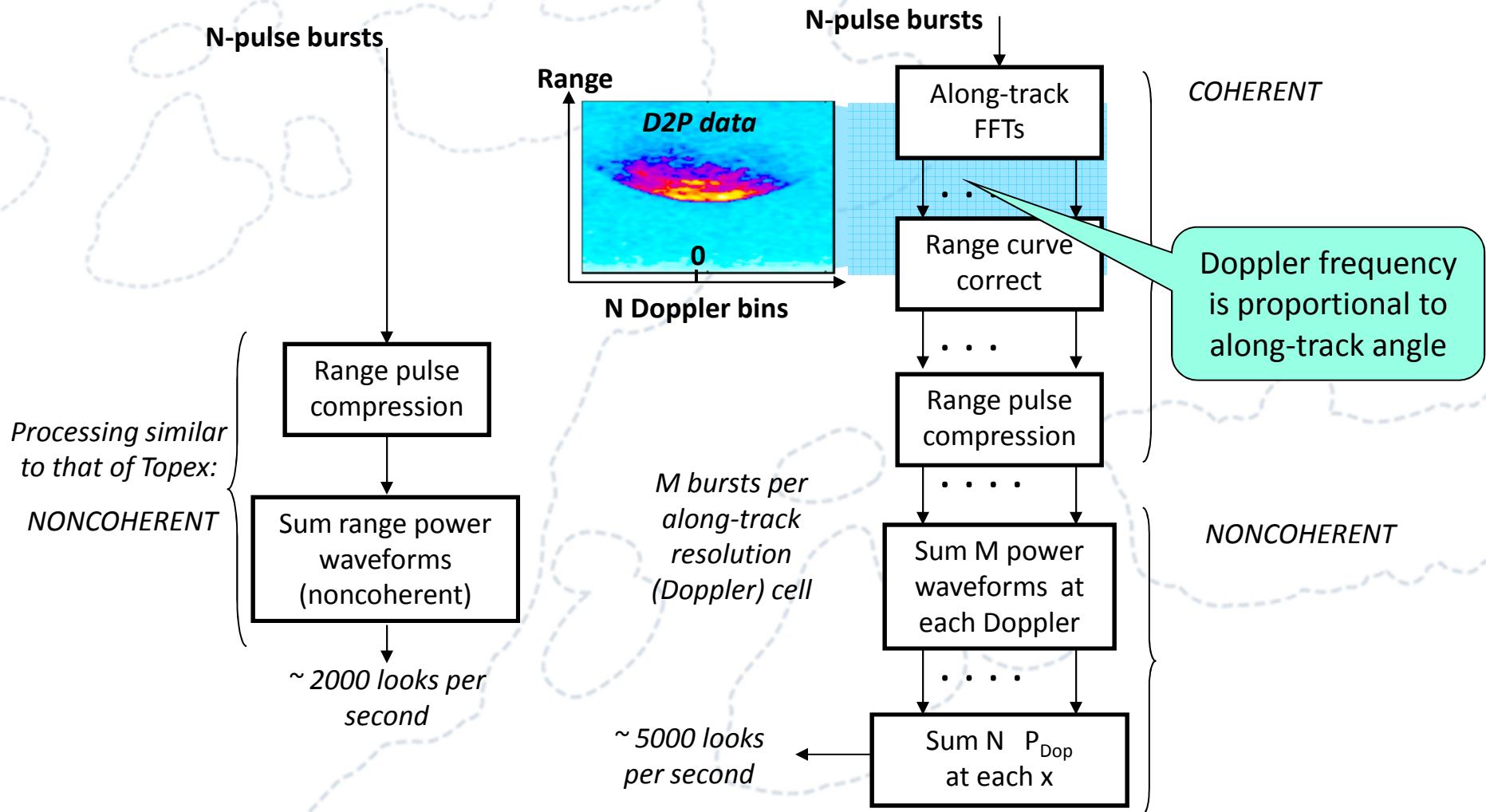


**Waveform rise time sharpness decreases in (quadratic) proportion to distance from nadir**

$$N_{\text{useful}} \approx \frac{2 h n \rho_{\text{rng}}}{X_{\text{Dop}}^2}$$

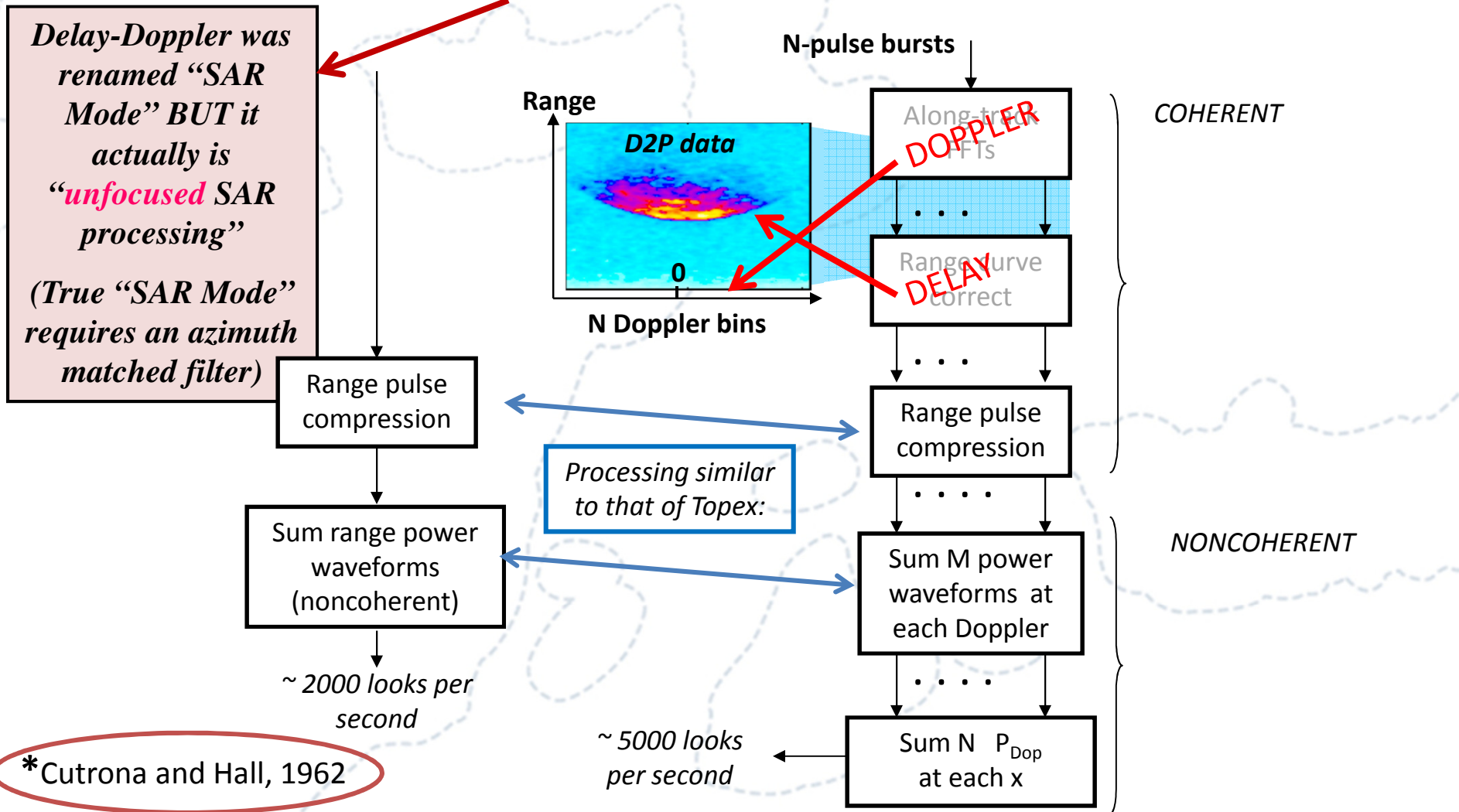


# DDA: *unfocused\** SAR mode Altimetry





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# Interleaved Mode

**(20yy): Jason-CS / Sentinel - 6**

**Open burst => interleaved Tx and Rx pulses**

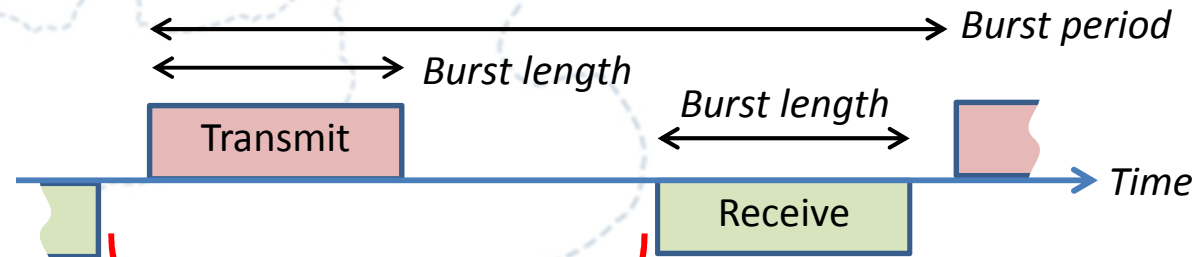
**Simultaneous unfocused SAR mode *and* LRM (*via decimation*)**

**Assures continuity with 22+ years of accumulated data**



# Closed Burst vs Open Burst

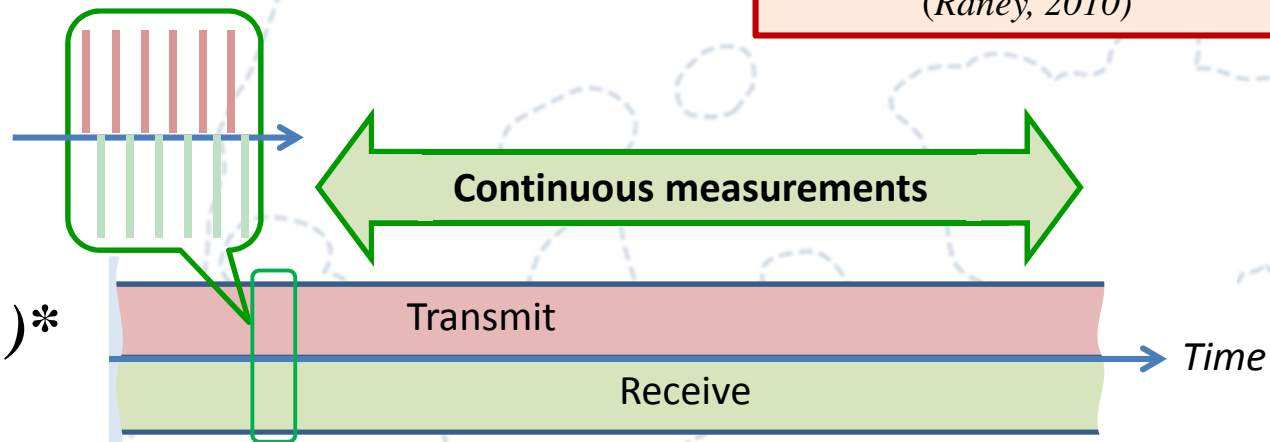
**Closed burst method**



**No measurements**

Closed burst disregards about 2/3 of the available CryoSat "listening" opportunities (Raney, 2010)

**Interleaved / Open burst (conventional!) method**



\*Precedent: TOPEX (Zieger et al, 1991)



# Maximum # of uncorrelated looks

*(unfocused SAR mode, interleaved)*

Number of looks per second (~10,000)

$$N_{sec} = N_{bin} N_{dt} N_{useful}$$

Maximum number of statistically independent looks within each Doppler bin

$$N_{bin} = \frac{2 \alpha X_{Dop}^2}{h \lambda}$$

*evaluated for the maximum burst repetition frequency (generalized Walsh bound)*

Number of Doppler bins (at nadir) traversed per second

$$N_{dt} = \frac{V_{sc}}{\alpha X_{Dop}}$$

$$\alpha = \frac{V_{sc}}{V_{foot}}$$



# A Fundamental Limit

( *unfocused interleaved SAR mode* )

- Open burst (=> interleaved mode) vs Closed burst  
*Interleaved mode, ideally with a quasi-continuous pulse-repetition frequency PRF,*
  - ✓ *maximizes the available “listening time”,*
  - ✓ *thus maximizing the number of available looks,*
  - ✓ *thus maximizing averaging,*
- thus minimizing the SSH measurement uncertainty (~ 5 mm @ Ku)

$$\langle \Delta r \rangle = \left( \frac{\lambda \rho_{rng} X_{Dop}}{4 n V_{sc}} \right)^{1/2}$$

*1<sup>st</sup> implementation : Jason-CS / Sentinel-6*





## Further possibilities (1 of 2) *of particular relevance to coastal altimetry*

### ➤ **Orbit selection**

*A non-repeat orbit (e.g. 1<sup>st</sup> 18 months of Geosat) would benefit geodesy, meet oceanographic requirements, and should be of interest for coastal applications*

### ➤ **Reduced cross-track footprint / selectivity**

*Two degrees of freedom in instrument design have yet to be investigated:*

*polarimetry (e.g., transmit CP, receive two orthogonal polarizations);*

*coherence \* (e.g., look for “persistent scatterers” in the sequence of backscattered signals, hence suppressing most land returns)*

\* Could be investigated using full waveform data





## Further possibilities (2 of 2) *of particular relevance to coastal altimetry*

### ➤ **Multi/wide swath altimetry**

*Such an instrument possibly will fly in future, but the achievable precision (averaging!) and effectiveness in near-shore environments have yet to be demonstrated*

**NB: The CryoSat-2 SARIn Mode could be exercised to explore this approach. For example, roll the s/c ~1.5 degrees to make it a nadir altimeter & side-looking imaging SAR interferometer; gather data over the ocean as well as over ocean/land scenes; estimate SSH of nadir & generate a near-nadir imaging swath**

### ➤ **Delay-Doppler vs (true) SAR mode**



N-pulse group  
(drawn from continuous interleaved sequence of received signals)

Along-track FFTs

...

Range curve correct

...

Range pulse compression

...

Azimuth pulse compression

...

Sum M powers  
 $P_{Bin}$  at each azimuth bin

...

Sum N  $P_{Dop}$  at each x

**True SAR-mode =>**  
*Azimuth focus*

COHERENT

What is the finest possible along-track resolution?

How many looks?

True SAR mode requires along-track focusing (matched filter and inverse FFTs) leading to smaller along-track resolved footprint  $X_{Dop}$

NONCOHERENT

Multi-look waveforms



## Precision vs Resolution

*Number of looks  $\times$  (1 / Resolution) < Constant*

A radar measurement **Uncertainty Principle**

*From information theory: resolution and statistically independent looks both require bandwidth (channel capacity)*

If all data are collected and processed through a true SAR mode focusing algorithm, the smallest along-track footprint is

$$D / 2\alpha = \rho_{at} \approx 0.5 \text{ m}$$

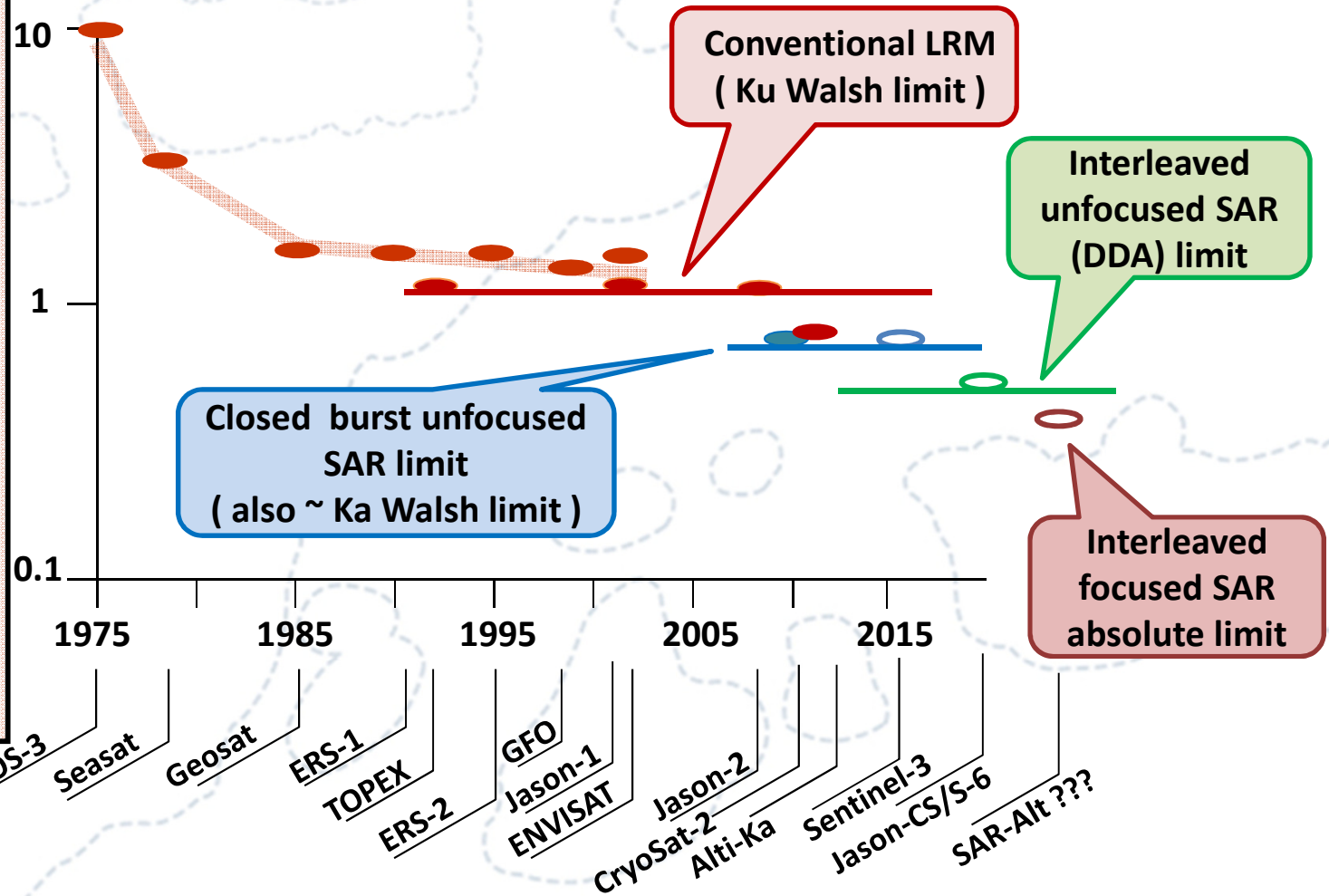
@ one look, which leads to the maximum number of looks per second

$$N_{SAR_{max}} = V_{foot} / \rho_{at} \approx 14,000$$

*Why? Small  $X_{Dop} \rightarrow \rho_{at}$  implies that all Doppler bins are “useful”*

# SSH (1-Hz) Precision Trends (cm)

Height **PRECISION** (instrument dependent) is the essential measurement attribute for geodesy, bathymetry, and mesoscale oceanography, and enhances near-shore measurements







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## Conclusions

- **Remarkable progress beyond LRM in the past 10 years**







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*Finer instrument precision => less averaging time needed*



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- **Unfocused SAR mode (DDA): significant milestone**  
*Especially for coastal applications: “beam-limited”*



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*Finer instrument precision => less averaging time needed*
- **Unfocused SAR mode (DDA): significant milestone**  
*Especially for coastal applications: “beam-limited”*
- **Focused SAR: smaller along-track resolution, more looks/sec**
- **Major milestone: Interleaved simultaneous DDA and LRM**
- **Twenty-five-year future milestone?**

*SAR-Alt: Focused nadir polarimetric SAR altimeter & side-looking SAR interferometer & LRM in non-repeating orbit*