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# Journal of Mathematics & Physics

22 (1943)  
 # [MTAC 20 465 66] vs

## TABLE OF COEFFICIENTS IN NUMERICAL INTEGRATION FORMULAE

BY A. N. LOWAN AND HERBERT SALZER

The values of  $B_n^{(n)}(1)/n!$  and  $B_n^{(n)}/n!$ , where  $B_n^{(n)}(1)$  denotes the  $n^{\text{th}}$  Bernoulli polynomial of the  $n^{\text{th}}$  order for  $x = 1$  and  $B_n^{(n)}$  denotes the  $n^{\text{th}}$  Bernoulli number of the  $n^{\text{th}}$  order, were computed for  $n = 1, 2, \dots, 20$ . The quantities  $B_n^{(n)}(1)/n!$  are required in the Laplace formula of numerical integration employing forward differences, as well as in the Gregory formula. The quantities  $B_n^{(n)}/n!$  are used in the Laplace formula employing backward differences. (See Milne-Thomson, "Calculus of Finite Differences", pp. 181-184, 191-193.)

$n$	$B_n^{(n)}(1)/n!$	$B_n^{(n)}/n!$
1	$\frac{1}{2}$	$-\frac{1}{2}$
2	$-\frac{1}{12}$	$\frac{5}{12}$
3	$\frac{1}{24}$	$-\frac{3}{8}$
4	$-\frac{19}{720}$	$\frac{251}{720}$
5	$\frac{3}{160}$	$-\frac{95}{288}$
6	$-\frac{863}{60480}$	$\frac{19087}{60480}$
7	$\frac{275}{24192}$	$-\frac{5257}{17280}$
8	$-\frac{33953}{3628800}$	$\frac{1070017}{3628800}$
9	$\frac{8183}{1036800}$	$-\frac{25713}{89600}$
10	$-\frac{3250433}{112001000}$	$\frac{26842253}{95800320}$
11	$\frac{4671}{788480}$	$-\frac{4777223}{17418240}$
12	$-\frac{13695779093}{2615348736000}$	$\frac{703604254357}{2615348736000}$
13	$\frac{2224234463}{475517952000}$	$-\frac{106364763817}{402361344000}$
14	$-\frac{132282840127}{31384184832000}$	$\frac{1166309819657}{4483454976000}$

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we can take  $|v_4| > 1$ .

$-v_4 + 4aM + a^2$ , and

$-G(-a)$ .

$+2G(a)$ .

$M^2 + 4a^3M$

$+2a^2 + G(a)$ .

$-4a^2 - 2G(a)$ .

increasing for  
 at  $P_{12}$  lies to the left  
 ves  $C$  of Theorem II.

↑  
 # these are called  
 "logarithmic numbers"

$n$	$B_n^{(n)}(1)/n!$				$B_n^{(n)}/n!$			
15	26396	51053			-25221	445		
	68976	23040	00		98402	304		
16	-11195	67034	48001		80929	89203	53324	9
	32011	86852	86400	00	32011	86852	86400	00
17	50188	465			-85455	47771	5379	
	15613	16556	8		34237	29254	40000	
18	-23340	28946	34446	3	12600	46723	60427	56559
	78601	44949	49376	000	51090	94217	17094	40000
19	30112	40351	85049		-13115	46499	95723	6437
	10928	54378	00448	000	53779	93912	81152	0000
20	-12365	72232	34699	80029	81368	36498	46758	25997
	48171	45976	18974	72000	00	33720	02183	33282
								30400
								000

NATIONAL BUREAU OF STANDARDS,  
MATHEMATICAL TABLES PROJECT, NEW YORK CITY

TABLE OF  $Ji_0(x)$ 

BY ARNOLD

Requests for the investigation of the integral in various tabular values of the function and related functions and an

## I. Derivation of Series E

From the known expansion

$$\int_x^\infty (J_0(t)/t) dt = \int_x^\infty \left[ (1 - \frac{1}{2}t^2 + \frac{1}{24}t^4 - \frac{1}{720}t^6 + \dots) \right]$$

where

$$K = \lim_{t \rightarrow \infty} \dots$$

To determine  $K$ , make

$$J_0(t)$$

Hence

$$Ji_0(x) =$$

Now

$$Ci(x) = - \int_x^\infty \frac{1}{t} dt$$

<sup>1</sup> The results reported here were prepared under the sponsorship of the National Bureau of Standards.

<sup>2</sup> The notation  $Ji_0(x)$  for this issue.