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A036040 tabf array: M_3 numbers of Abramowitz and Stegun.

Partitions of n listed in Abramowitz-Stegun order p. 831-2 (see the main page for the reference).

n\k	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	...
1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3	1	3	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
4	1	4	3	6	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
5	1	5	10	10	15	10	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
6	1	6	15	10	15	60	15	20	45	15	1	0	0	0	0	0	0	0	0	0	0	0	0
7	1	7	21	35	21	105	70	105	35	210	105	35	105	21	1	0	0	0	0	0	0	0	0
8	1	8	28	56	35	28	168	280	210	280	56	420	280	840	105	70	560	420	56	210	28	1	
.																							
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n\k	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	...

The next two rows, for n=9 and 10 are:

[1, 9, 36, 84, 126, 36, 252, 504, 315, 378, 1260, 280, 84, 756, 1260, 1890, 2520, 1260, 126, 1260, 840, 3780, 945, 126, 1260, 1260, 84, 378, 36, 1]

[1, 10, 45, 120, 210, 126, 45, 360, 840, 1260, 630, 2520, 1575, 2100, 120, 1260, 2520, 1575, 3780, 12600, 2800, 3150, 6300, 210, 2520, 4200, 9450, 12600, 12600, 945, 252, 3150, 2100, 12600, 4725, 210, 2520, 3150, 120, 630, 45, 1]

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A(t) = exp(x[k]*(t^k)/k! ,k=1..infinity) is the exponential generating function (e.g.f.) of the n-variate polynomials P3_n(x[1],...,x[n]) with p(n):=A000041(n)(partition numbers) terms.

These polynomials are, for n=1,...,10:

- n=1: 1*x[1]
- n=2: 1*x[2] +1*x[1]^2
- n=3: 1*x[3] +3*x[1]*x[2] +1*x[1]^3
- n=4: 1*x[4] +4*x[1]*x[3] +3*x[2]^2 +6*x[1]^2*x[2] +1*x[1]^4
- n=5: 1*x[5] +5*x[1]*x[4] +10*x[2]*x[3] +10*x[1]^2*x[3] +15*x[1]*x[2]^2 +10*x[1]^3*x[2] +1*x[1]^5
- n=6: 1*x[6] +6*x[1]*x[5] +15*x[2]*x[4] +10*x[3]^2 +15*x[1]^2*x[4] +60*x[1]*x[2]*x[3] +15*x[2]^3 +20*x[1]^3*x[3] +45*x[1]^2*x[2]^2 +15*x[1]^4*x[4] +1*x[1]^6
- n=7: 1*x[7] +7*x[1]*x[6] +21*x[2]*x[5] +35*x[3]*x[4] +21*x[1]^2*x[5] +105*x[1]*x[2]*x[4] +70*x[1]*x[3]^2 +105*x[2]^2*x[3] +35*x[1]^3*x[4] +210*x[1]^2*x[2]*x[3] +105*x[1]*x[2]^3 +35*x[1]^4*x[3] +105*x[1]^3*x[2]^2 +21*x[1]^5*x[2] +1*x[1]^7

n=8: $1*x[8] + 8*x[1]*x[7] + 28*x[2]*x[6] + 56*x[3]*x[5] + 35*x[4]^2 + 28*x[1]^2*x[6] + 168*x[1]*x[2]*x[5]$
 $+ 280*x[1]*x[3]*x[4] + 210*x[2]^2*x[4] + 280*x[2]*x[3]^2 + 56*x[1]^3*x[5] + 420*x[1]^2*x[2]*x[4]$
 $+ 280*x[1]^2*x[3]^2 + 840*x[1]*x[2]^2*x[3] + 105*x[2]^4 + 70*x[1]^4*x[4] + 560*x[1]^3*x[2]*x[3]$
 $+ 420*x[1]^2*x[2]^3 + 56*x[1]^5*x[3] + 210*x[1]^4*x[2]^2 + 28*x[1]^6*x[2] + 1*x[1]^8$

n=9: $1*x[9]$
 $+ 9*x[1]*x[8] + 36*x[2]*x[7] + 84*x[3]*x[6] + 126*x[4]*x[5]$
 $+ 36*x[1]^2*x[7] + 252*x[1]*x[2]*x[6] + 504*x[1]*x[3]*x[5] + 315*x[1]*x[4]^2 + 378*x[2]^2*x[5]$
 $+ 1260*x[2]*x[3]*x[4] + 280*x[3]^3$
 $+ 84*x[1]^3*x[6] + 756*x[1]^2*x[2]*x[5] + 1260*x[1]^2*x[3]*x[4] + 1890*x[1]*x[2]^2*x[4]$
 $+ 2520*x[1]*x[2]*x[3]^2 + 1260*x[2]^3*x[3]$
 $+ 126*x[1]^4*x[5] + 1260*x[1]^3*x[2]*x[4] + 840*x[1]^3*x[3]^2 + 3780*x[1]^2*x[2]^2*x[3]$
 $+ 945*x[1]*x[2]^4$
 $+ 126*x[1]^5*x[4] + 1260*x[1]^4*x[2]*x[3] + 1260*x[1]^3*x[2]^3$
 $+ 84*x[1]^6*x[3] + 378*x[1]^5*x[2]^2$
 $+ 36*x[1]^7*x[2]$
 $+ 1*x[1]^9$

n=10: $1*x[10]$
 $+ 10*x[1]*x[9] + 45*x[2]*x[8] + 120*x[3]*x[7] + 210*x[4]*x[6] + 126*x[5]^2$
 $+ 45*x[1]^2*x[8] + 360*x[1]*x[2]*x[7] + 840*x[1]*x[3]*x[6] + 1260*x[1]*x[4]*x[5]$
 $+ 630*x[2]^2*x[6] + 2520*x[2]*x[3]*x[5] + 1575*x[2]^2*x[4]^2 + 2100*x[3]^2*x[4]$
 $+ 120*x[1]^3*x[7] + 1260*x[1]^2*x[2]*x[6] + 2520*x[1]^2*x[3]*x[5] + 1575*x[1]^2*x[4]^2$
 $+ 3780*x[1]*x[2]^2*x[5] + 12600*x[1]*x[2]*x[3]*x[4] + 2800*x[1]*x[3]^3 + 3150*x[2]^3*x[4]$
 $+ 6300*x[2]^2*x[3]^2$
 $+ 210*x[1]^4*x[6] + 2520*x[1]^3*x[2]*x[5] + 4200*x[1]^3*x[3]*x[4] + 9450*x[1]^2*x[2]^2*x[4]$
 $+ 12600*x[1]^2*x[2]*x[3]^2 + 12600*x[1]*x[2]^3*x[3] + 945*x[2]^5$
 $+ 252*x[1]^5*x[5] + 3150*x[1]^4*x[2]*x[4] + 2100*x[1]^4*x[3]^2 + 12600*x[1]^3*x[2]^2*x[3]$
 $+ 4725*x[1]^2*x[2]^4$
 $+ 210*x[1]^6*x[4] + 2520*x[1]^5*x[2]*x[3] + 3150*x[1]^4*x[2]^3$
 $+ 120*x[1]^7*x[3] + 630*x[1]^6*x[2]^2$
 $+ 45*x[1]^8*x[2]$
 $+ 1*x[1]^10$

e.o.f.