



製造業の現場と自動運転の未来を支えるソフトウェア技術

研究成果及び技術の概要紹介

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国立情報学研究所 アーキテクチャ科学研究系 教授
同 数理的高信頼ソフトウェアシステム研究センター長

総合研究大学院大学 情報学専攻

JST ERATO 蓮尾メタ数理システムデザインプロジェクト 研究総括

自己紹介

- 数学 > 数学基礎論・応用数学 > 数理論理学
- 数学 > 代数学 > 圏論
- 情報学 > ソフトウェア > ソフトウェア科学・形式検証・数理論理学

- 東大 数学 (学士)
 - > 東工大 数理・計算 (修士)
 - > Radboud U. Nijmegen 計算機科学 (PhD)
 - > 京大数理研 (助教)
 - > 東大 コンピュータ科学専攻 (講師・准教授)
 - > 国立情報研 (准教授・教授)

- さきがけ 西浦領域 (2007-2011)

共著書： 圏論の歩き方
(日本評論社, 2015)



研究チーム紹介

- 国立情報学研究所 数理的高信頼ソフトウェアシステム研究センター：
ソフトウェア分野の包括的研究グループ

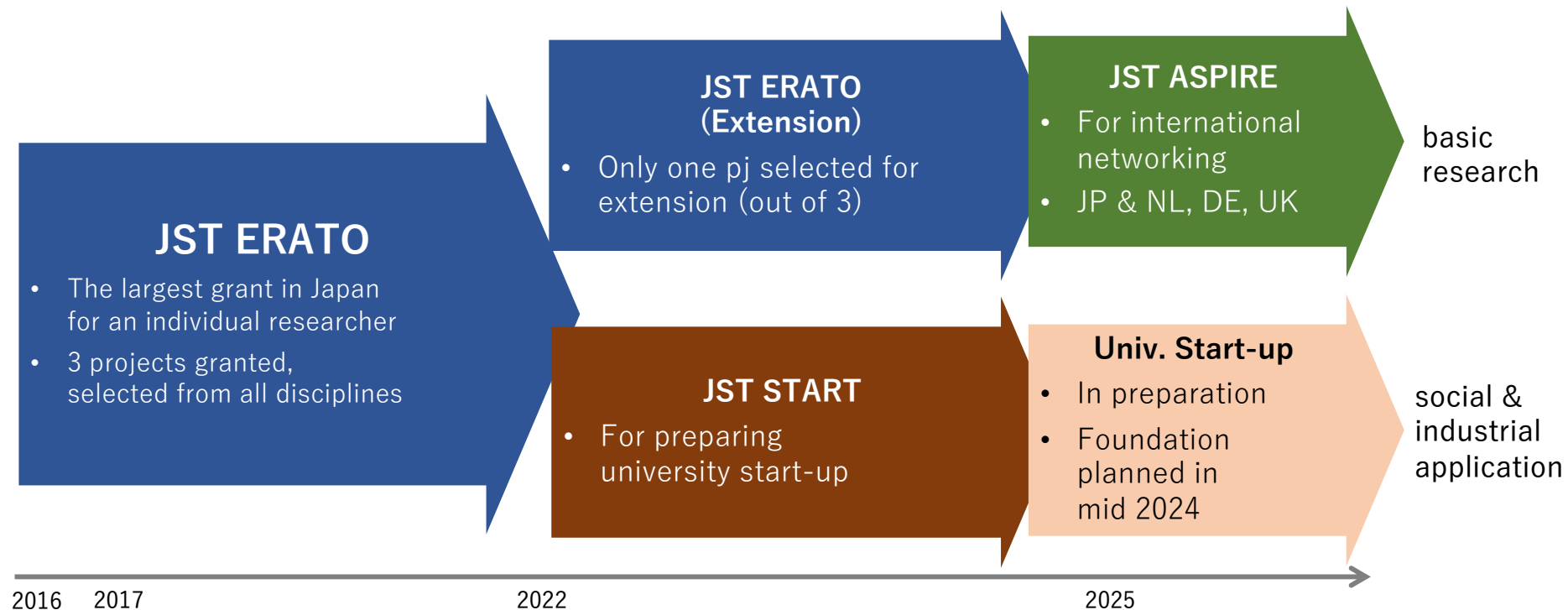
- 研究員 7
- 博士課程学生 6
- プログラマー 2

- JST funding

- 基礎研究
- 国際展開
- 産業化支援

- 数学のチカラを
社会に示す

- 数学基礎論
- 代数学



自動運転・生成AIなどの新情報技術は「侵襲的」 社会受容を支える技術で、人間中心の情報化社会へ

ブラックボックス 「安全性」

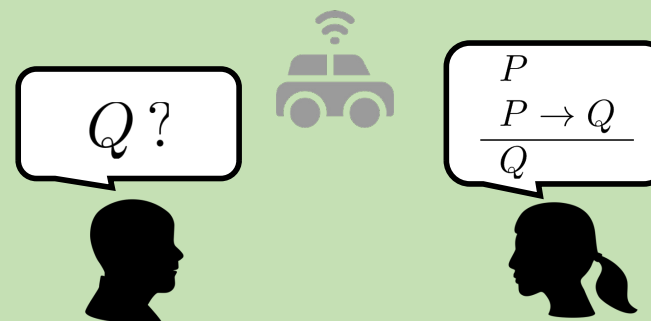


- 中身の見えない「安全性主張」
- 精査・批判的検討・改良・責任所在の議論が困難

↑ 現状の多く

VS

説明可能安全性



- 説明可能でトレーサブルな論理的な安全性主張
- 実世界の安全性保証は終わりのない営為、対話による社会全体の取り組みをサポート
→ 情報技術への社会的信頼，社会受容
→ 本格展開，真の情報化社会の実現

↑ ソフトウェア科学・論理学を使い
我々の追求する未来像

— 新情報技術の社会受容を可能にする数学 —

- 2024年6月19日 (水) 11:30~20:30
(受付開始 11:00)
- 参加登録締め切り：今日
- 「蓮尾 erato シンポジウム」で検索

新情報技術の
社会受容を
可能にする数学

JST ERATO
蓮尾メタ数理システムデザイン
プロジェクト (ERATO MMSD)
成果報告会



2024年6月19日(水)
11:30-20:00
一橋講堂 (東京都千代田区一ツ橋)
参加無料・要事前登録

Software Science in Manufacturing Industry: Historical Perspective & Overview

Formal methods for (conventional) software

(e.g. model checking)

Goal:

to *prove* $\mathcal{M} \models \varphi$

- “A system \mathcal{M} satisfies a req./spec./property φ ”
- Conventionally:
 \mathcal{M} is a program
 φ is “bug-free”
→ *bug-free proofs*

```
'replace_interests' => false,  
'send_welcome' => false,  
})  
on_error('error', {result}) {  
  on_result = array ('response'=>'error', 'message'  
  {  
    on_result = array ('response'=>'success');  
  }  
  on_send($arrResult);  
}
```

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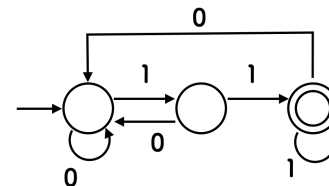
```
'replace_interests' => false,  
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on_error('error', {result}) {  
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{  
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  }  
  on_send($errResult);  
}
```

Heavy-weight formal methods for manufacturing

Goal:

to *prove* $\mathcal{M} \models \varphi$

- \mathcal{M} is a car
 φ is safety/quality/...
- But **we need a
mathematical/logical
model \mathcal{M} of a car!**



Modeling is costly

- MBD usually doesn't help...
Simulink is for numeric simulation,
not principally for logical verification

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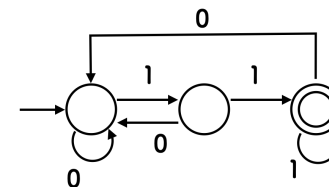
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Light-weight formal methods

→ *Manufacturing DX*

- Formal/math./software
description of φ
- Feasible yet powerful

Proof-based

mathematical traffic laws
for automated driving

- For int'l safety standards,
a sound ecosystem,
& social acceptance

Software Science in Manufacturing Industry: Historical Perspective & Overview

Part 1

Formal methods for (conventional) software

(e.g. model checking)

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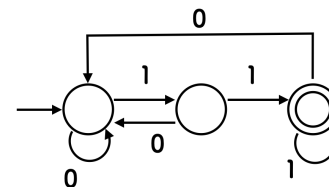
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Light-weight formal methods

→ *Manufacturing DX*

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Part 2

Proof-based

mathematical traffic laws
for automated driving

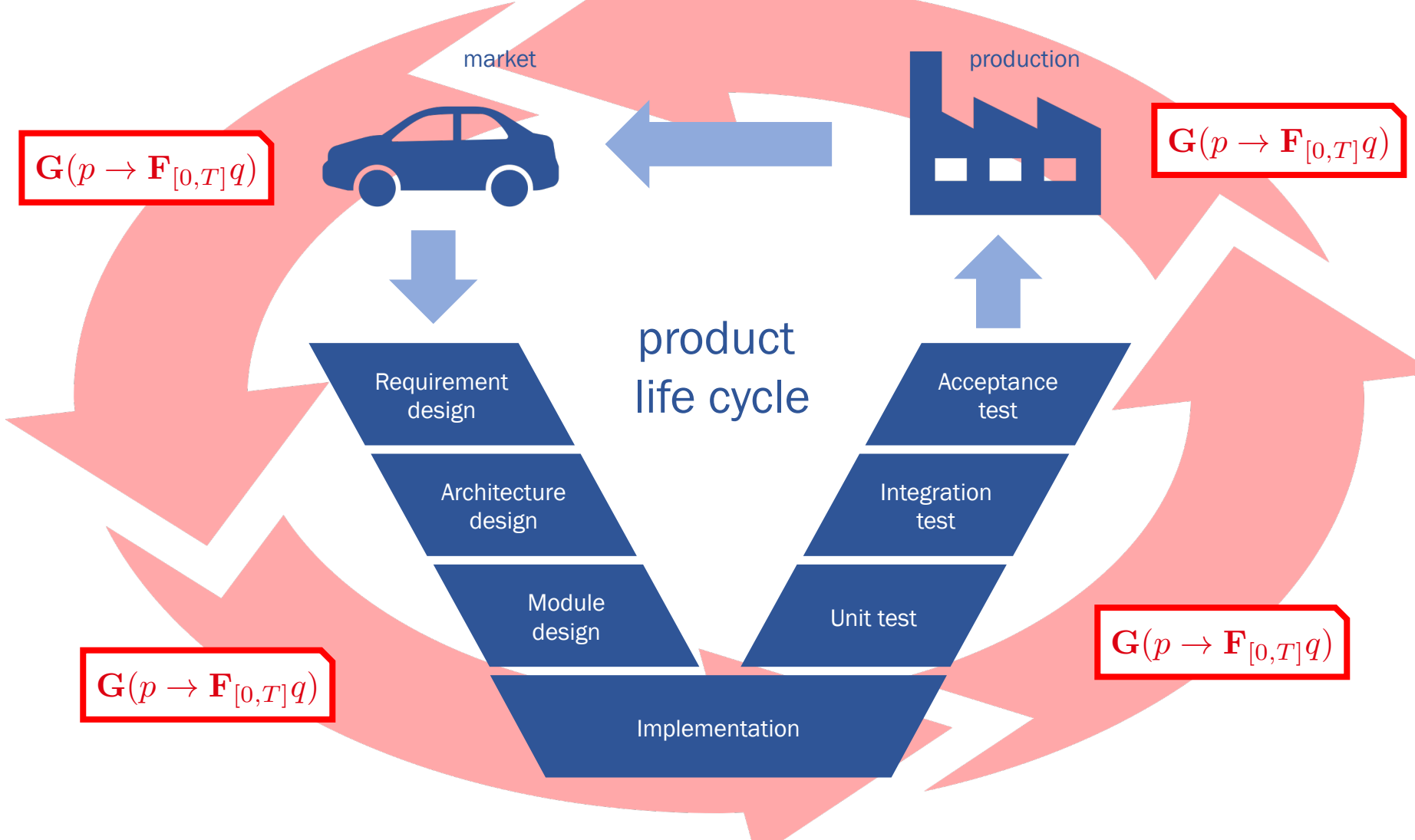
- For int'l safety standards, a sound ecosystem, & social acceptance

Part 1

Specification Driven Engineering: **Its Concept and Tool Support**

Collaboration w/ Mitsubishi Electric, Mitsubishi Heavy Industry, TOYOTA, ...

Design, V&V, Production, and Deployment— Underpinned by Shared Formal Specifications



- automation
- inter-operability
- communicability
- traceability
- responsibility

Benefits...

- within each phase
- in connecting different phases

Rigorous and Unambiguous Definition of “What Is Needed”

Formal specification

$$\mathbf{G}(p \rightarrow \mathbf{F}_{[0,T]} q)$$

written in a formal language
such as STL

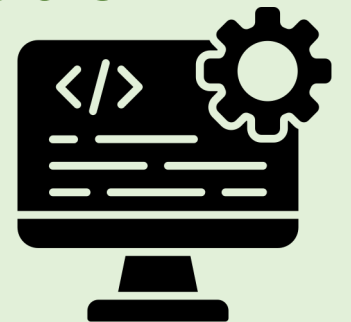
$$\varphi ::= \alpha \mid \neg\varphi \mid \varphi_1 \vee \varphi_2 \mid \\ \mathbf{F}_I\varphi \mid \varphi_1 \mathbf{U}_I\varphi_2$$

- 1. Its meaning is mathematically defined.**
No ambiguity, no dispute

$$\begin{aligned} \sigma \models \alpha &\iff f(\sigma(0)) \geq 0 && (\sigma \models \perp \text{ never holds}) \\ \sigma \models \neg\varphi &\iff \sigma \not\models \varphi \\ \sigma \models \varphi_1 \wedge \varphi_2 &\iff \sigma \models \varphi_1 \text{ and } \sigma \models \varphi_2 \\ \sigma \models \varphi_1 \mathbf{U}_I \varphi_2 &\iff \exists t \in I. (\sigma^t \models \varphi_2 \wedge \forall t' \in [0, t). \sigma^{t'} \models \varphi_1) \\ \sigma \models \varphi_1 \mathbf{R}_I \varphi_2 &\iff \forall t \in I. (\sigma^t \not\models \varphi_2 \Rightarrow \exists t' \in [0, t). \sigma^{t'} \models \varphi_1) \end{aligned}$$

- 2. Machine processable.**

*Write, record,
inspect, and use
it in software*



Spec: “What is Needed”

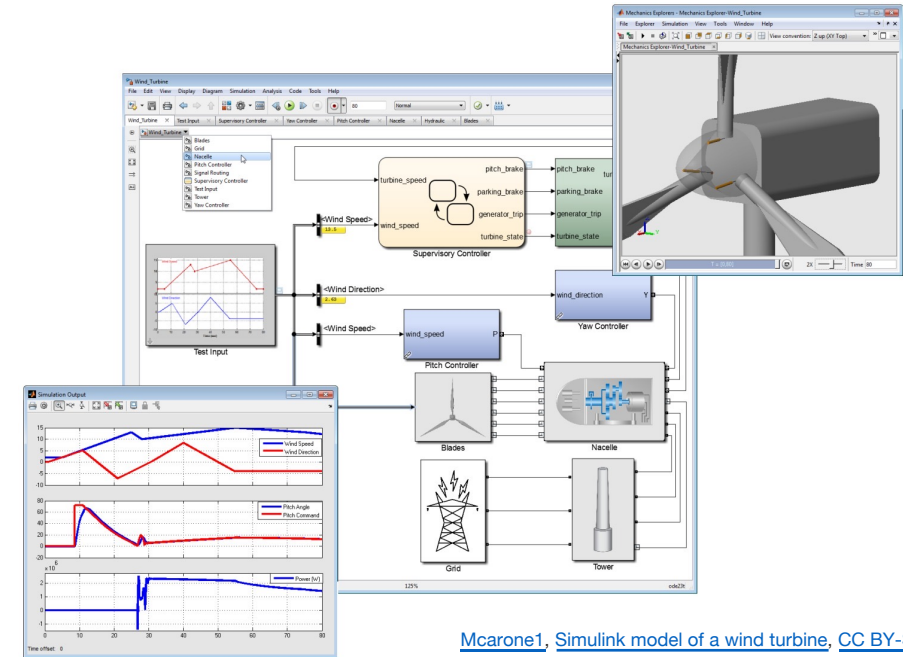
Model: “How Spec is Realized”

Specs:

$$G(\text{gear} = 1 \wedge \text{rpm} > 3500 \Rightarrow F[0,1] \text{ gear} = 2)$$

“When gear is 1st and rpm is > 3500, then gear will be 2nd within 1 sec.”

Models:



Mcarone1, Simulink model of a wind turbine, CC BY-SA 3.0

Disturbance scenarios of ISO 34502 [Reimann, Mansion et al., SAC 2024]

Road sector	Subject-vehicle behaviour	Cut in	Cut out	Acceleration	Deceleration (Stop)
Main roadway	Lane keep	No.1	No.2	No.3	No.4
	Lane change	No.5	No.6	No.7	No.8
Merge zone	Lane keep	No.9	No.10	No.11	No.12
	Lane change	No.13	No.14	No.15	No.16
Departure zone	Lane keep	No.17	No.18	No.19	No.20
	Lane change	No.21	No.22	No.23	No.24

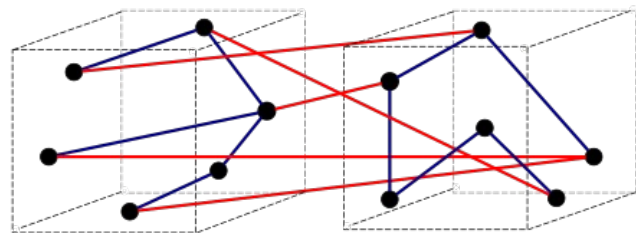
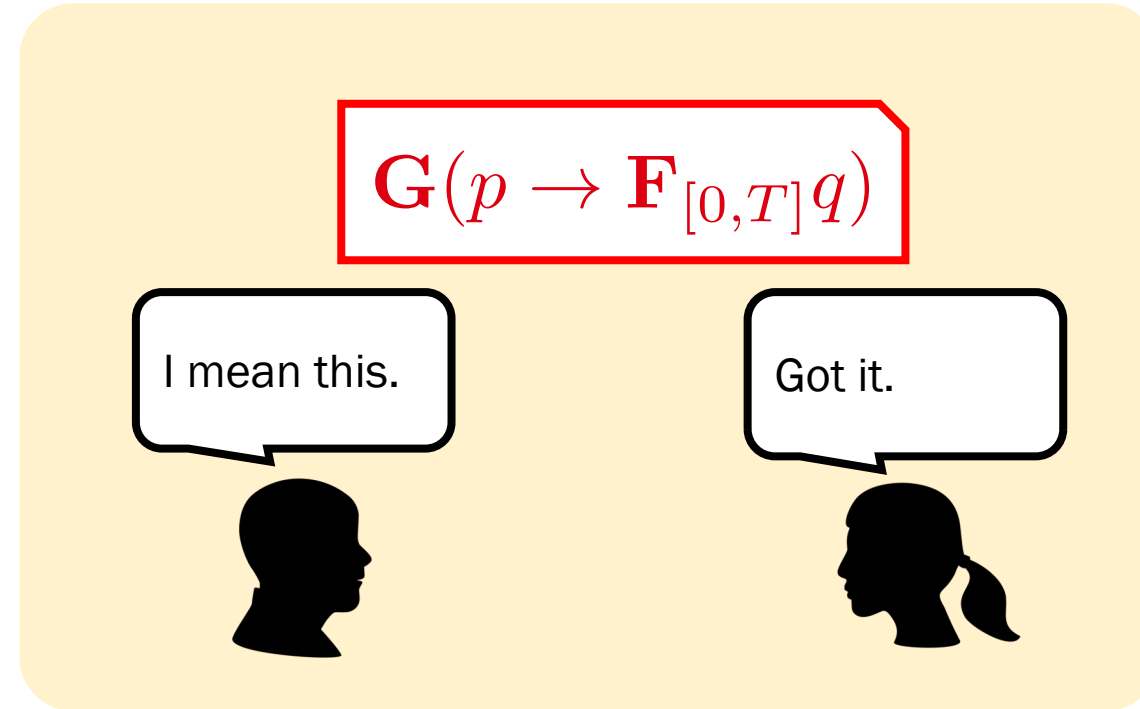
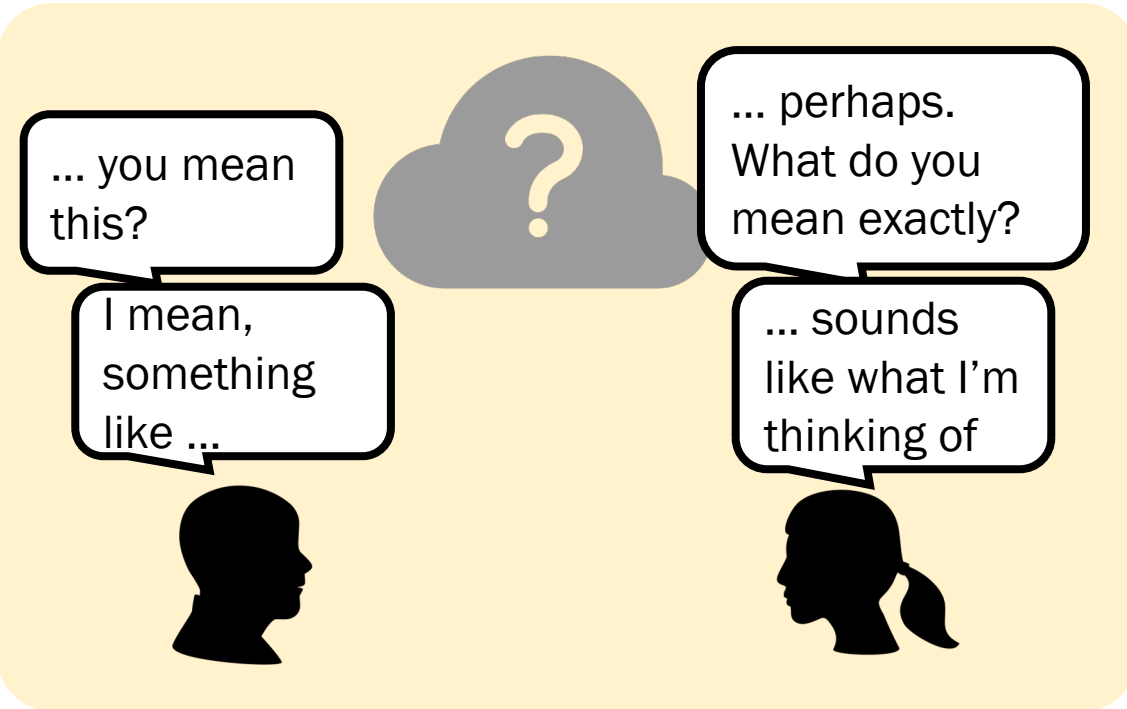
$\text{scenario}(SV, POV, L) \equiv \text{initSafe}(SV, POV) \wedge \text{roadSector}(SV, POV) \wedge \text{disturb}(SV, POV, L), i = 1, \dots, 24$ (cf. this is (1). initSafe is from §4.3)
 $\text{disturb}(SV, POV, L) \equiv \text{initialCondition}(SV, POV, L) \wedge \text{behaviourSV}_i(SV, L) \wedge \text{behaviourPOV}_i(SV, L), i = 1, \dots, 24$ (cf. §2) in §3)

i	roadSector, (cf. §4.1)	i	initialCondition, (cf. §4.2)	behaviourSV _{<i>i</i>} , (cf. §4.4)	behaviourPOV _{<i>i</i>} , (cf. §4.5)
1	Main roadway	1	T	laneKeep(SV, L) $\mathcal{U} \text{ danger}(SV, POV)$	cutIn(POV, SV)
2		sameLanes(SV, POV ₁ , POV ₂ , L) $\wedge \text{aheadOf}(SV, POV_1)$ $\wedge \text{aheadOf}(POV_1, POV_2)$	laneKeep(SV, L) $\wedge \text{laneKeep}(POV_2, L)$ $\mathcal{U}(\sim \text{sameLane}(SV, POV_1, L))$	leavingLane(POV ₁ , L) $\wedge \text{laneKeep}(POV_2, L)$ $\mathcal{U}(\sim \text{sameLane}(POV_2, POV_1, L))$	
3	Merge zone	3	aheadOf(POV, SV) $\wedge \text{sameLane}(SV, POV, L)$ $\vee \text{inAdjLanes}(SV, POV, L)$	laneKeep(SV, L) $\mathcal{U} \text{ danger}(SV, POV)$	accel(POV, SV, L) $\mathcal{U} \text{ danger}(SV, POV)$
4		aheadOf(SV, POV) $\wedge \text{sameLane}(SV, POV, L)$ $\vee \text{inAdjLanes}(SV, POV, L)$	laneKeep(SV, L) $\mathcal{U} \text{ danger}(SV, POV)$	decel(POV, SV, L) $\mathcal{U} \text{ danger}(SV, POV)$	
5-8	Departure zone	5	T	leavingLane(SV, L)	cutIn(POV, SV)
6		T	leavingLane(SV, L)	cutOut(POV, SV, L)	
7		aheadOf(POV, SV)	enteringLane(SV, L)	accel(POV, SV, L) $\mathcal{U} \text{ danger}(SV, POV)$	
8		sameLanes(SV, L) $\wedge \text{aheadOf}(SV, POV)$	leavingLane(SV, L)	decel(POV, SV, L) $\mathcal{U} \text{ danger}(SV, POV)$	
9-16	mergeZone(SV, POV)	9-16	initialCondition ₉₋₁₆	behaviourSV ₉₋₁₆	behaviourPOV ₉₋₁₆
17-24	departZone(SV, POV)	17-24	initialCondition ₁₇₋₂₄	behaviourSV ₁₇₋₂₄	behaviourPOV ₁₇₋₂₄

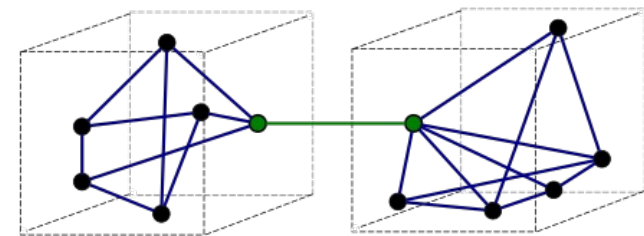
- In temporal logic, state machines, etc.
- One-line (top) to ~50 lines (bottom)

- In Simulink, Modelica, MapleSim, ...
- Takes time and cost to build (months)

Communication on Solid and Unambiguous Bases



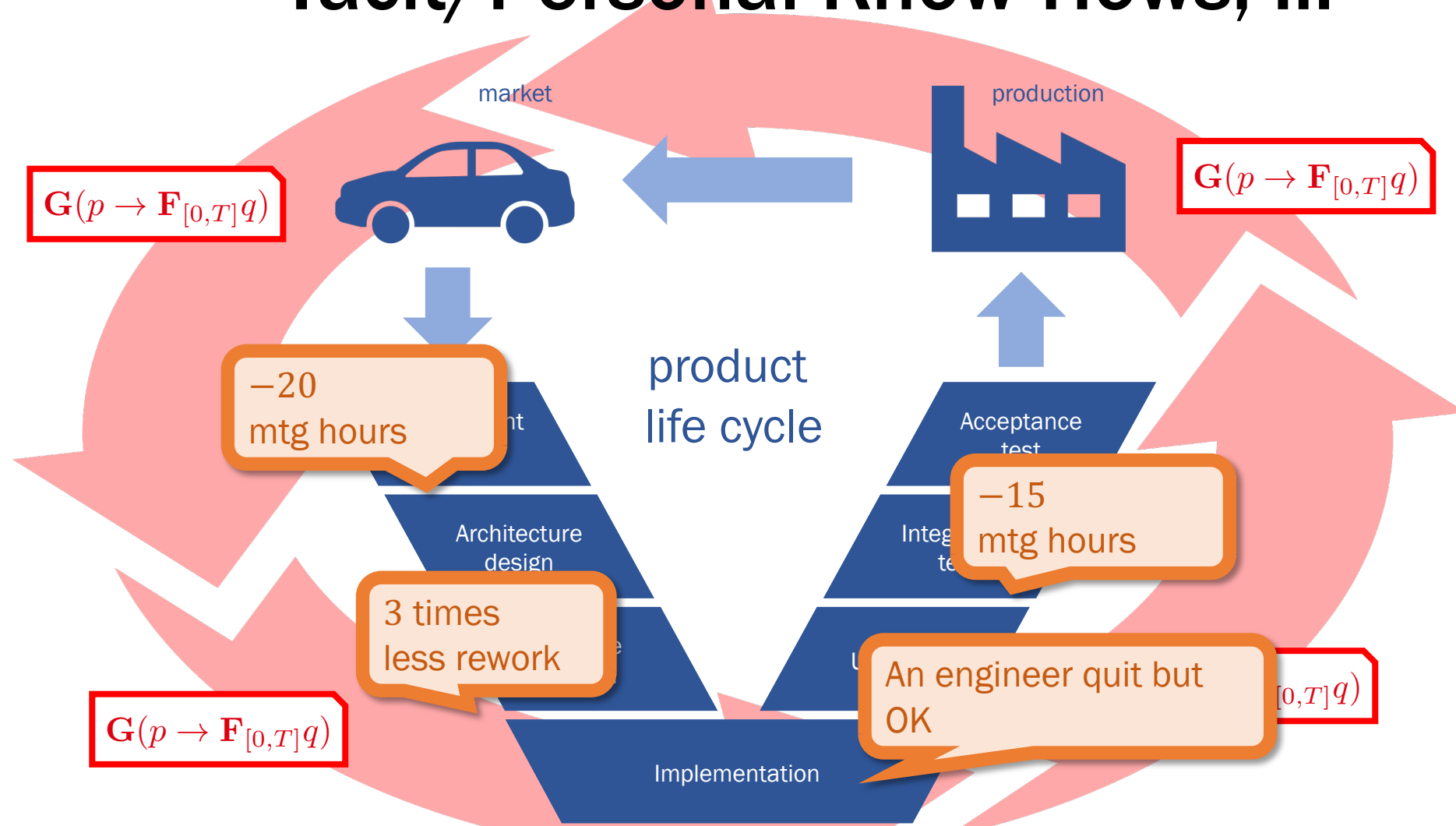
b) Bad (high coupling, low cohesion)



a) Good (loose coupling, high cohesion)

"Low Coupling, High Cohesion"

Reducing Meetings, Reworks, Tacit/Personal Know-Hows, ...



Automating Daily Analysis Tasks, Reducing Person-Hours

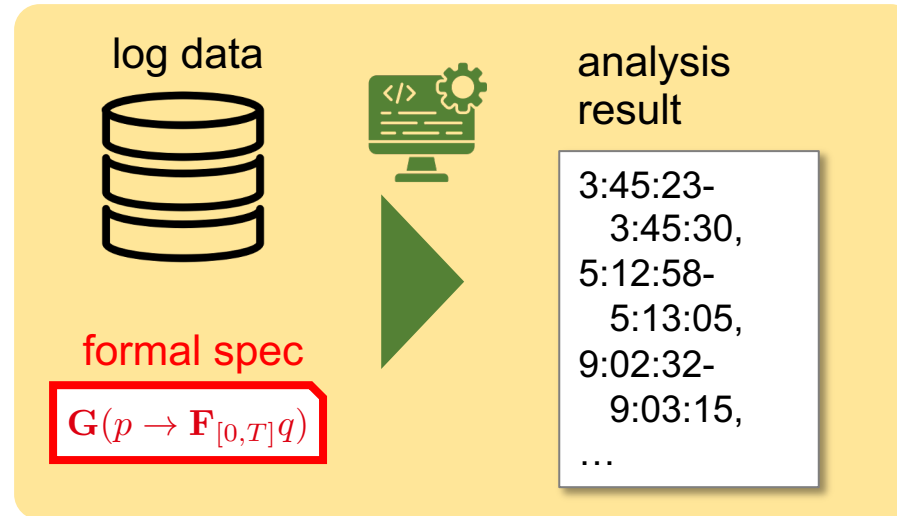
Task example: log extraction

Collab. w/



Where in the log does a dangerous passing occur?

[Reimann, Mansion, et al., SAC'24]



BEFORE:

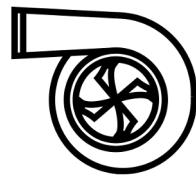
- Tens of hours of manual inspection or ad-hoc C-coding

AFTER: w/ our algorithm

- Automated & fast analysis (100K events/sec.)
- User effort is minimal (writing a logical formula, < 10 lines)

Task example: parameter optimization

Collab. w/

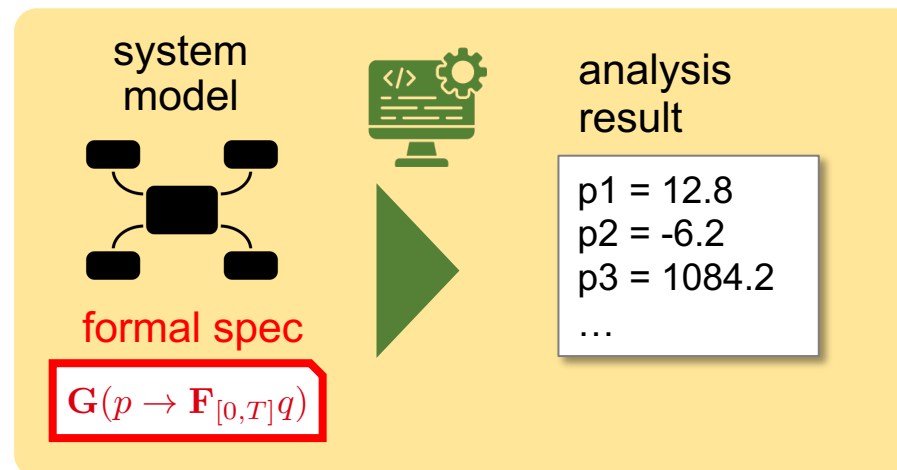


gas turbine for power plants



Need to tune parameter values for safety and efficiency

[Sato+, FM'21]



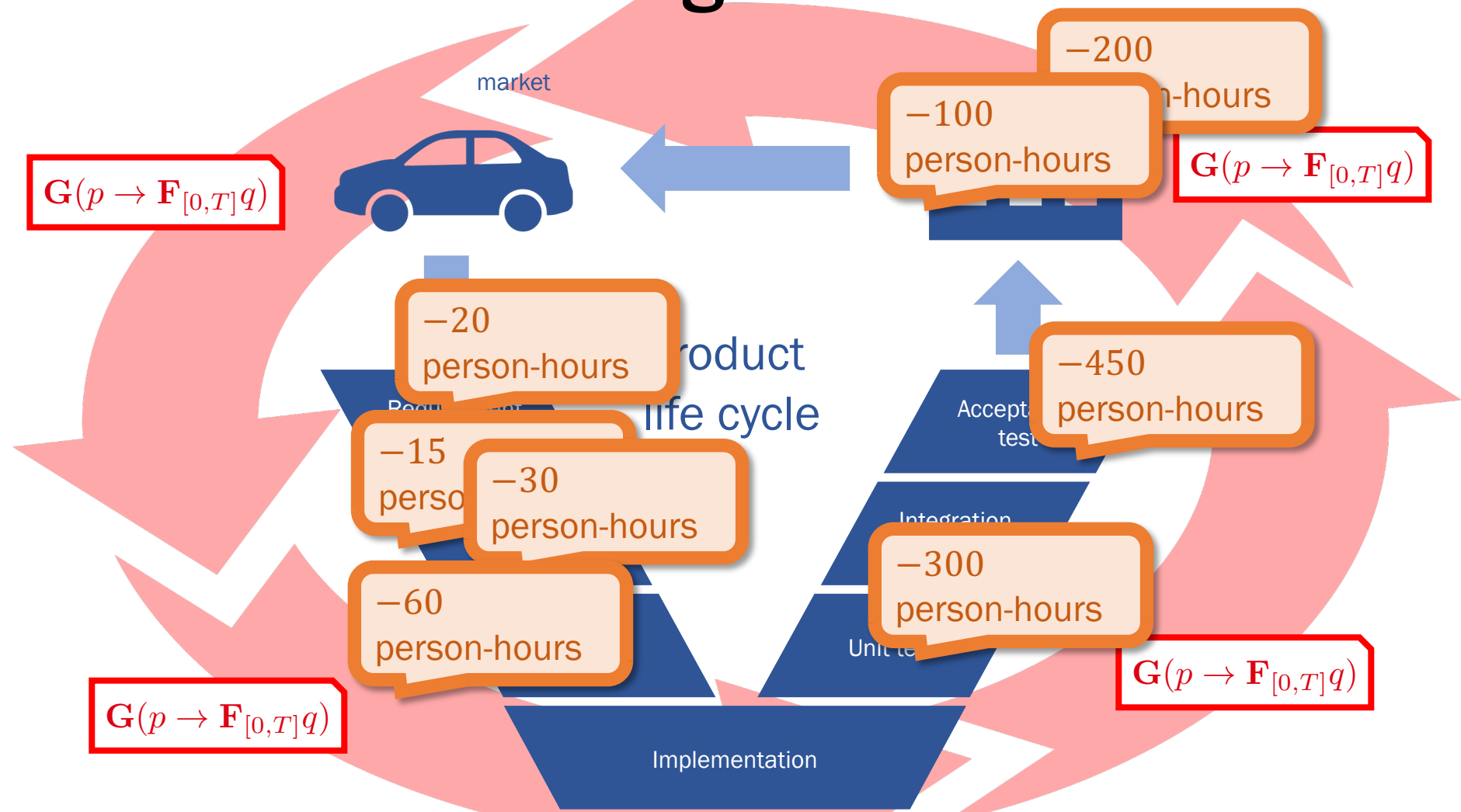
BEFORE:

- Manual efforts by experts (7 man-days in [Sato+, FM'21])

AFTER: w/ our algorithm

- Automated & fast analysis (3 hrs in [Sato+, FM'21])
- Better answer

Automating Daily Analysis Tasks, Reducing Person-Hours



Writing and Managing Formal Specs Is Not Easy

Formal specification

$$\mathbf{G}(p \rightarrow \mathbf{F}_{[0,T]}q)$$

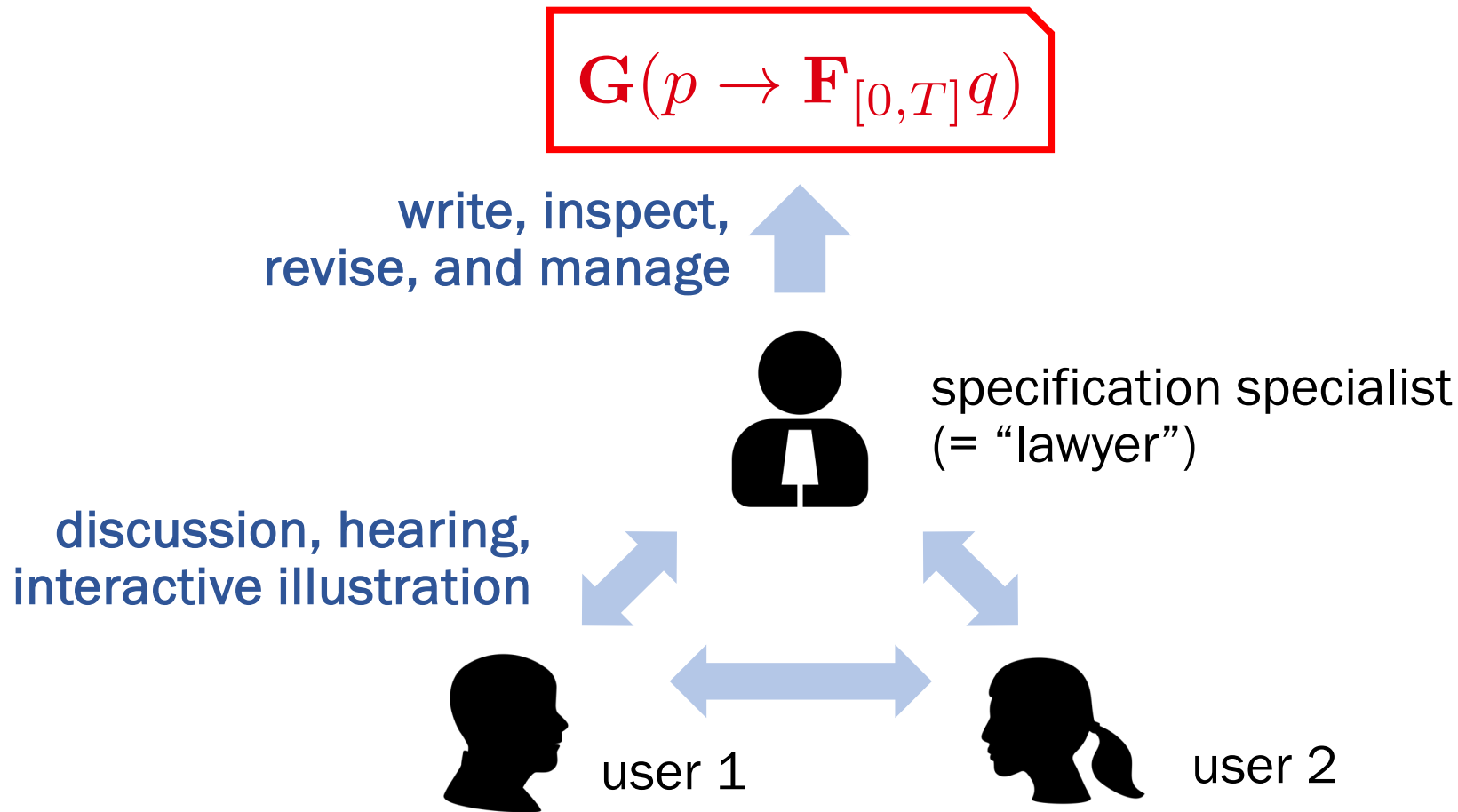
written in a formal language
such as STL

$$\varphi ::= \alpha \mid \neg\varphi \mid \varphi_1 \vee \varphi_2 \mid \\ \mathbf{F}_I\varphi \mid \varphi_1 \mathbf{U}_I\varphi_2$$

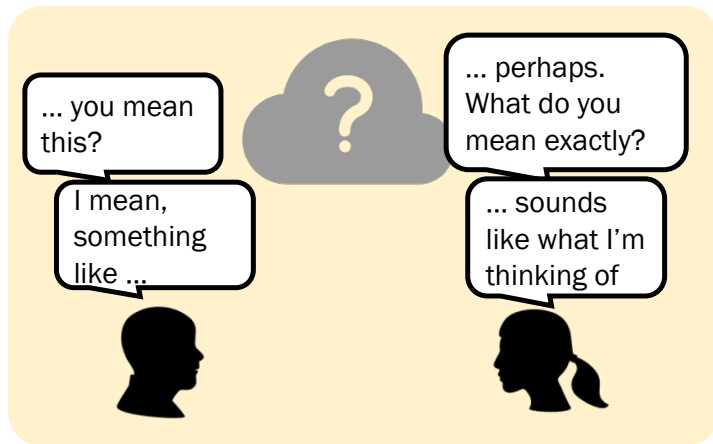
I'm not a
mathematician...



The *Lawyer Model* for Formal Specifications

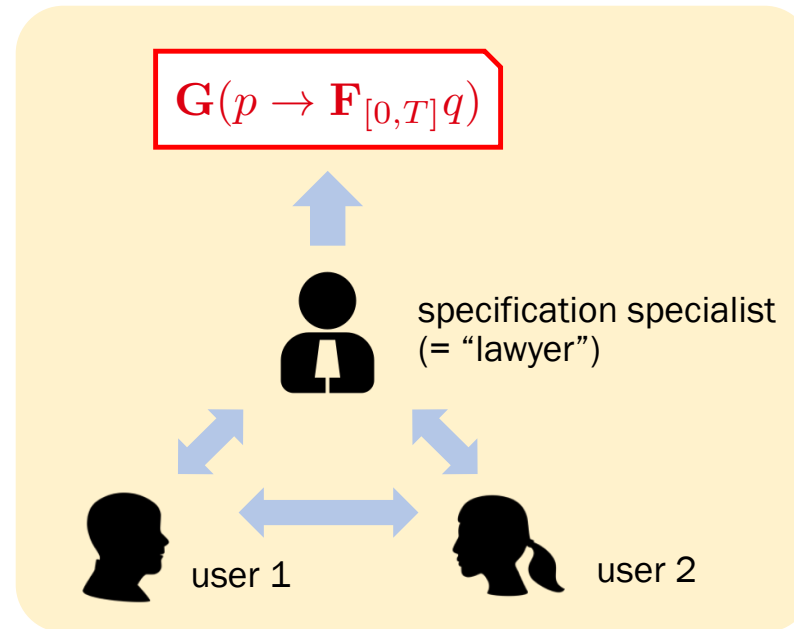


The *Lawyer Model* for Formal Specifications



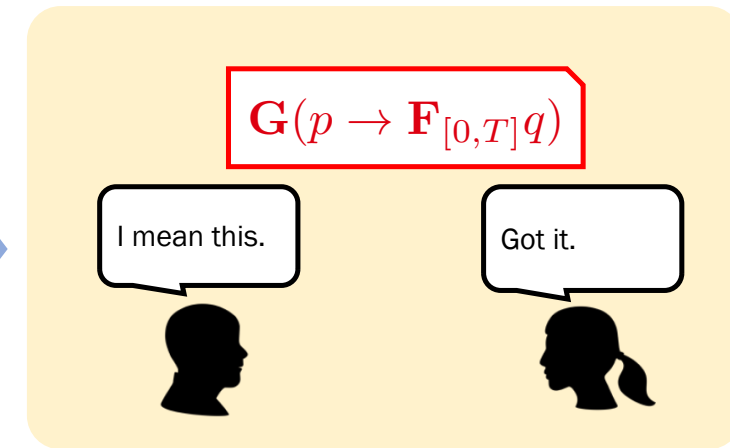
Current practice

expensive



The lawyer model
(our immediate goal)

admissible comm. cost
and feasible now



Communication
in formal specs
(our ultimate goal)

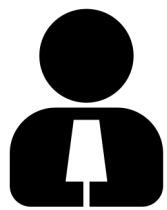
cheap comm. cost but
learning cost is needed

The *Lawyer Model* for Formal Specifications and Its Software Support

It does cost, but history points to this

$$G(p \rightarrow F_{[0,T]}q)$$

write, inspect, revise, and manage



specification specialist (= "lawyer")

discussion, hearing, interactive illustration



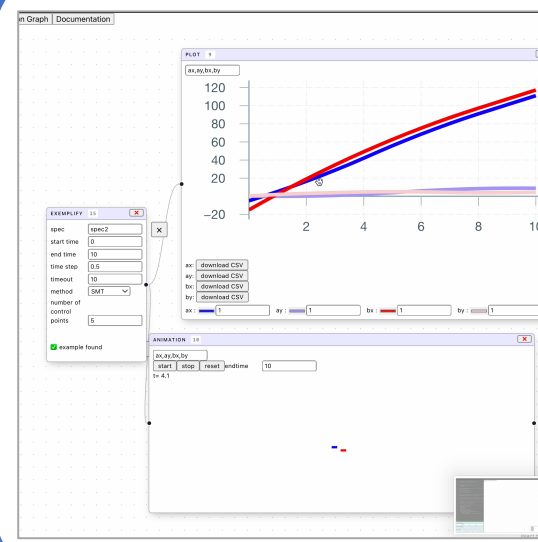
user 1



user 2

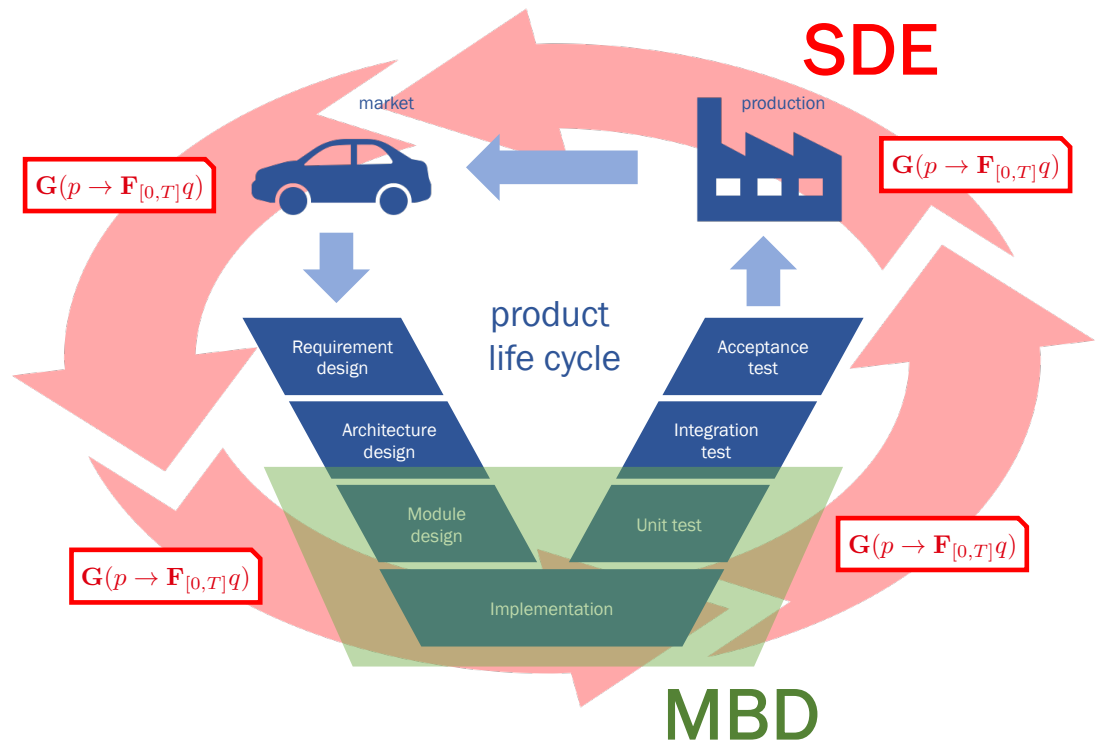
```
25
26 def spec1(ax: Real, ay: Real, bx: Real, by: Real): Bool =
27   (always assu(ax,ay,bx,by))
28   ^ aheadOf(bx,ax)
29   ^ ay == by
30   ^ (always atLane(bx,by,0))
31   ^ safe_init(ax,ay,bx,by)
32   ^ (atLane(ax,ay,0) ^ atLane(bx,by,0)) U [0,5]
33     (danger(ax,ay,bx,by)
34      ^ (eventually[0,3] (always atLane(ax,ay,1))))
35
36
37
38
39
40
41
42
43 // second trial, with "danger" tightened
44 def danger_tight(ax: Real, ay: Real, bx: Real, by: Real): B
45   abs(ax-bx) ≤ 7 ^ abs(ay-by) ≤ 3
46
47 def safe_init_tight(ay: Real, ay: Real, by: Real, by: Real)
```

spec editor
(IDE for formal specs)



interactive spec illustrator
(visual illustration of formal specs)

Mutually Complementary Paradigms towards Responsible & Efficient Manufacturing



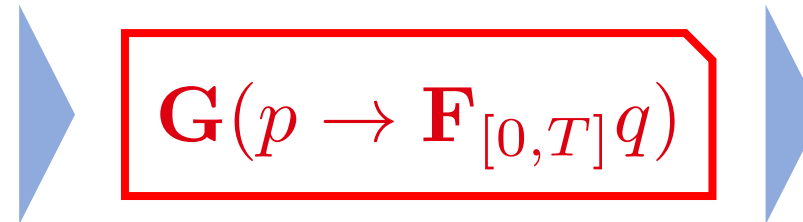
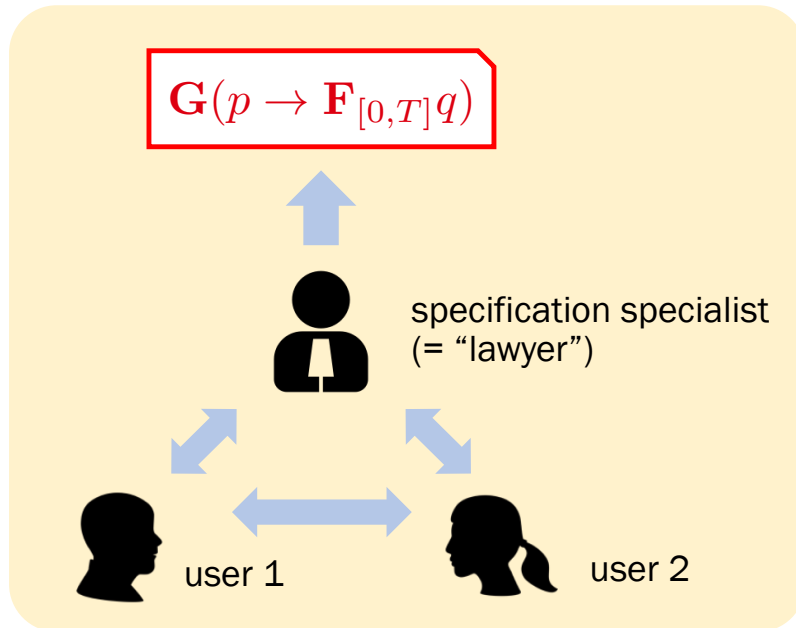
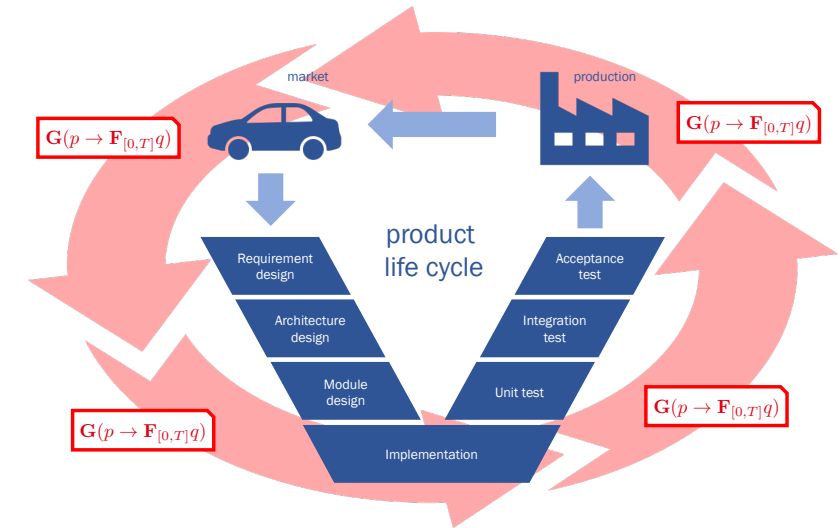
V&V asks mechanized in MBD ↓ mechanized in SDE ↓
 if a system (model) **M** satisfies a spec **φ**

	MBD	SDE
target phases	design, impl., V&V	the whole product life cycle
requirement	system model (costly)	formal spec (cheaper)
advantage	model → V&V → impl. (eliminating rework)	<ul style="list-style-type: none"> V&V automation communicability traceability

Part 1 (Specification-Driven Engineering)

Summary

The SDE workflow—
supported by tools from software science!



A formal spec:

an unambiguous and
machine-processable
description of requirements
and contracts

<p>Task example: log extraction</p> <p>Collab. w/ MITSUBISHI ELECTRIC</p> <p>[Reimann, Mansion, et al., SAC'24]</p>	<p>log data</p> <p>formal spec $G(p \rightarrow F_{[0,T]}q)$</p> <p>Where in the log does a dangerous passing occur?</p>	<p>analysis result</p> <p>3:45:23-3:45:30, 5:12:58-5:13:05, 9:02:32-9:03:15, ...</p>	<p>BEFORE:</p> <ul style="list-style-type: none"> Tens of hours of manual inspection or ad-hoc C-coding <p>AFTER: w/ our algorithm</p> <ul style="list-style-type: none"> Automated & fast analysis (100K events/sec.) User effort is minimal (writing a logical formula, < 10 lines)
<p>Task example: parameter optimization</p> <p>Collab. w/ MITSUBISHI HEAVY INDUSTRIES</p> <p>[Sato+, FM21]</p>	<p>gas turbine for power plants</p> <p>formal spec $G(p \rightarrow F_{[0,T]}q)$</p> <p>Need to tune parameter values for safety and efficiency</p>	<p>system model</p> <p>analysis result</p> <p>p1 = 12.8, p2 = -6.2, p3 = 1084.2, ...</p>	<p>BEFORE:</p> <ul style="list-style-type: none"> Manual efforts by experts (7 man-days in [Sato+, FM21]) <p>AFTER: w/ our algorithm</p> <ul style="list-style-type: none"> Automated & fast analysis (3 hrs in [Sato+, FM21]) Better answer

- automation
- inter-operability
- communicability
- traceability
- responsibility

Software Science in Manufacturing Industry: Historical Perspective & Overview

Part 1

Formal methods for (conventional) software

(e.g. model checking)

Goal:

to *prove* $\mathcal{M} \models \varphi$

- “A system \mathcal{M} satisfies a req./spec./property φ ”
- Conventionally: \mathcal{M} is a program
 φ is “bug-free”
→ *bug-free proofs*

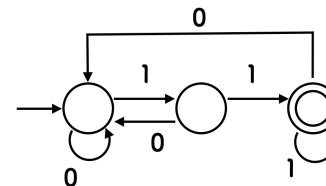
```
'replace_interests' => false,
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})
on_error('error', {result}) {
  on_result = array ('response'=>'error', 'message'
  on_result = array ('response'=>'success!');
  on_send($errResult);
```

Heavy-weight formal methods for manufacturing

Goal:

to *prove* $\mathcal{M} \models \varphi$

- \mathcal{M} is a car
 φ is safety/quality/...
- But **we need a mathematical/logical model \mathcal{M} of a car!**



Modeling is costly

- MBD usually doesn't help
- Simulink is for numeric simulation, not for logical verification

Light-weight formal methods

→ *Manufacturing DX*

- Formal/math./software description of φ
- Feasible yet powerful

Part 2

Proof-based

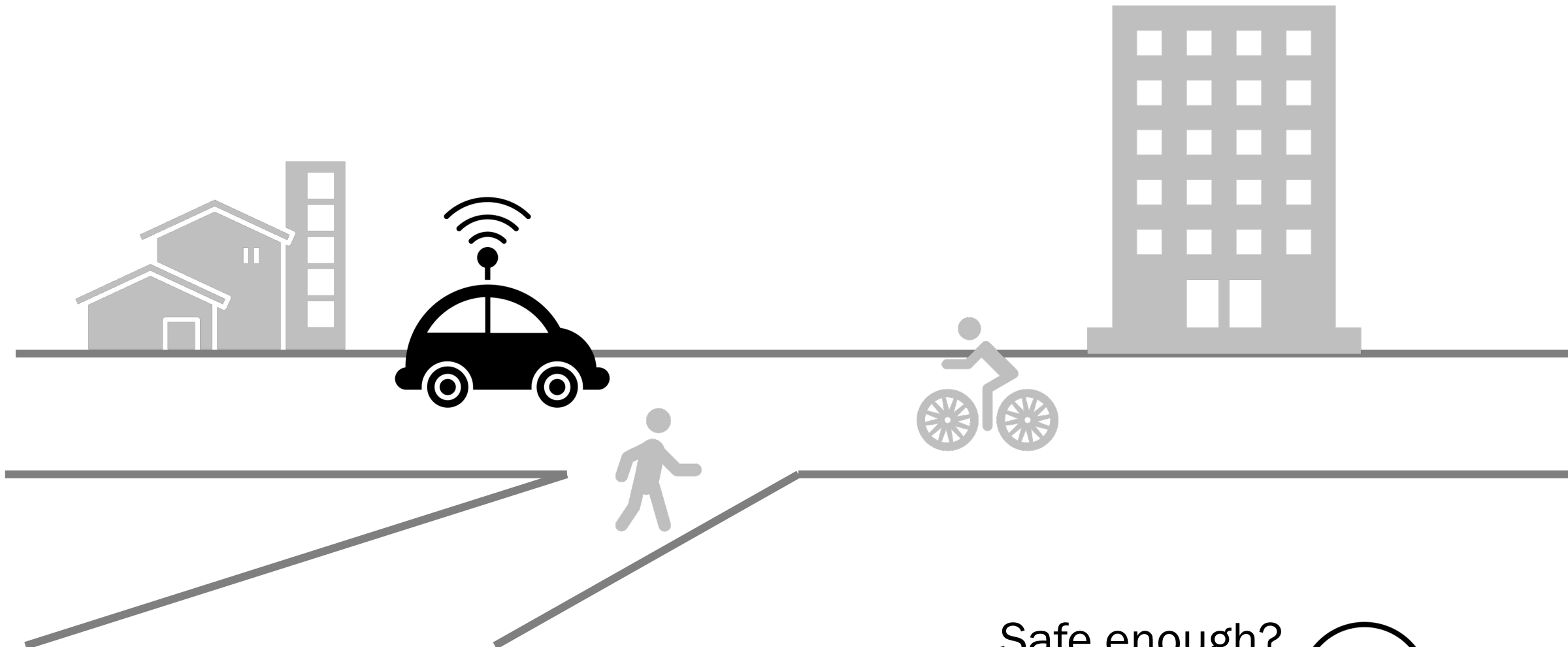
mathematical traffic laws
for automated driving

- For int'l safety standards, a sound ecosystem, & social acceptance

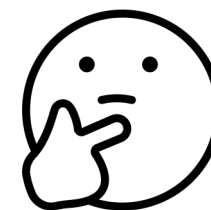
Part 2

Proof-based *Mathematical Traffic Laws* for Automated Driving

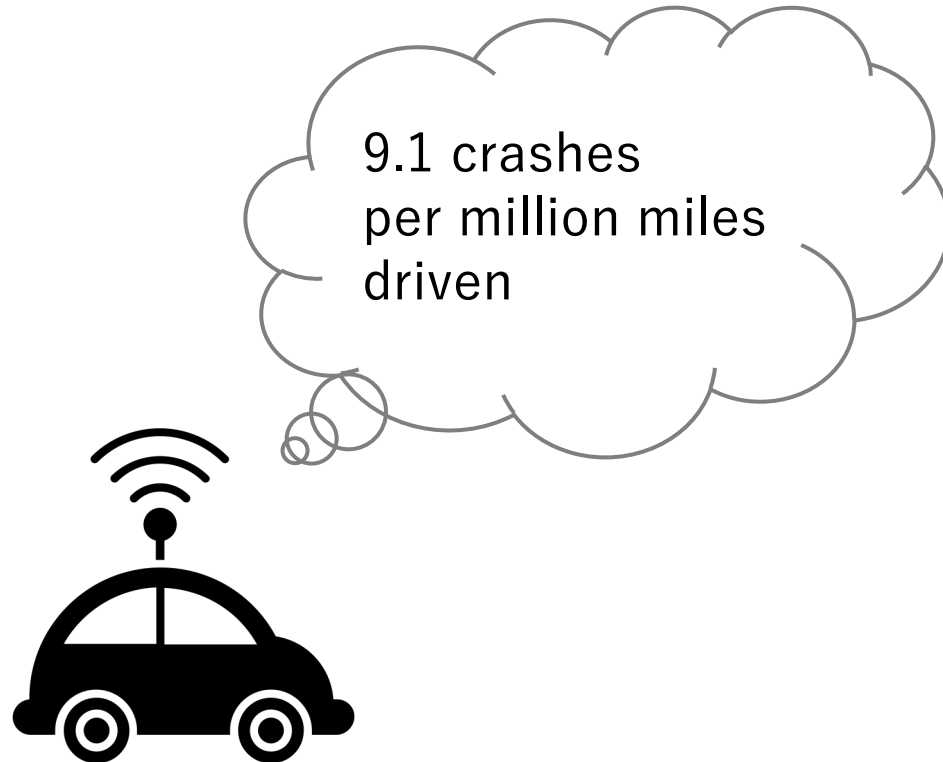
Collaboration w/ Mazda, ...
Standardization efforts at IEEE SA, ...



Safe enough?



Guarantee by statistical data



Guarantee by testing and simulation



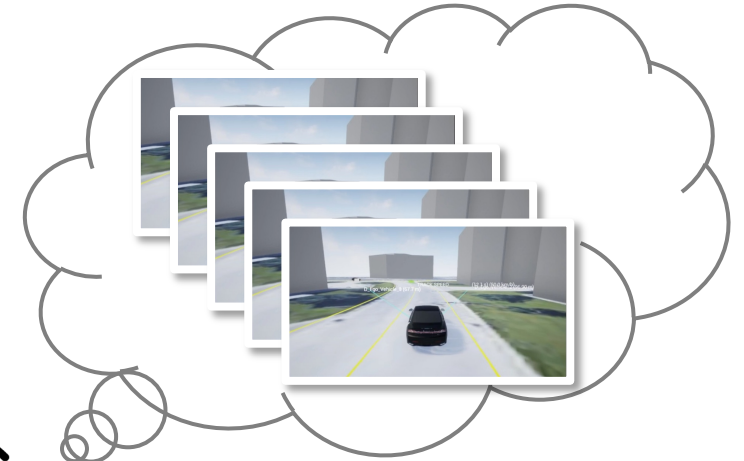
Guarantee strong enough?

Guarantee
by statistical data

9.1 crashes
per million miles
driven



Guarantee
by testing and simulation



Explainability?

Proof.

We prove the first statement. The rest is shown symmetrically.

Let $S \subseteq L$ be an arbitrary subset. We let S^\downarrow be the set of lower bounds of S , that is,

$$S^\downarrow := \{y \in L \mid y \sqsubseteq s \text{ for each } s \in S\}$$

Since $S^\downarrow \subseteq L$ is a subset of L , it has its supremum in the semilattice (L, \sqsubseteq) . We claim that $\bigsqcup S^\downarrow$ is the infimum of S .

To prove the claim, it suffices to show the two-way characterization in (2.1), that is, we need to show

$$\frac{y \sqsubseteq s \text{ for each } s \in S}{y \sqsubseteq \bigsqcup S^\downarrow}.$$

For the downward implication in ??,

$$\begin{aligned} y \sqsubseteq s \text{ for each } s \in S & \\ \implies y \in S^\downarrow & \quad \text{by def. of } S^\downarrow \\ \implies y \sqsubseteq \bigsqcup S^\downarrow & \quad \text{since } \bigsqcup S^\downarrow \text{ is an upper bound of } S^\downarrow \end{aligned}$$

For the upward implication in ??, we first observe

$$\bigsqcup S^\downarrow \sqsubseteq s \text{ for each } s \in S.$$

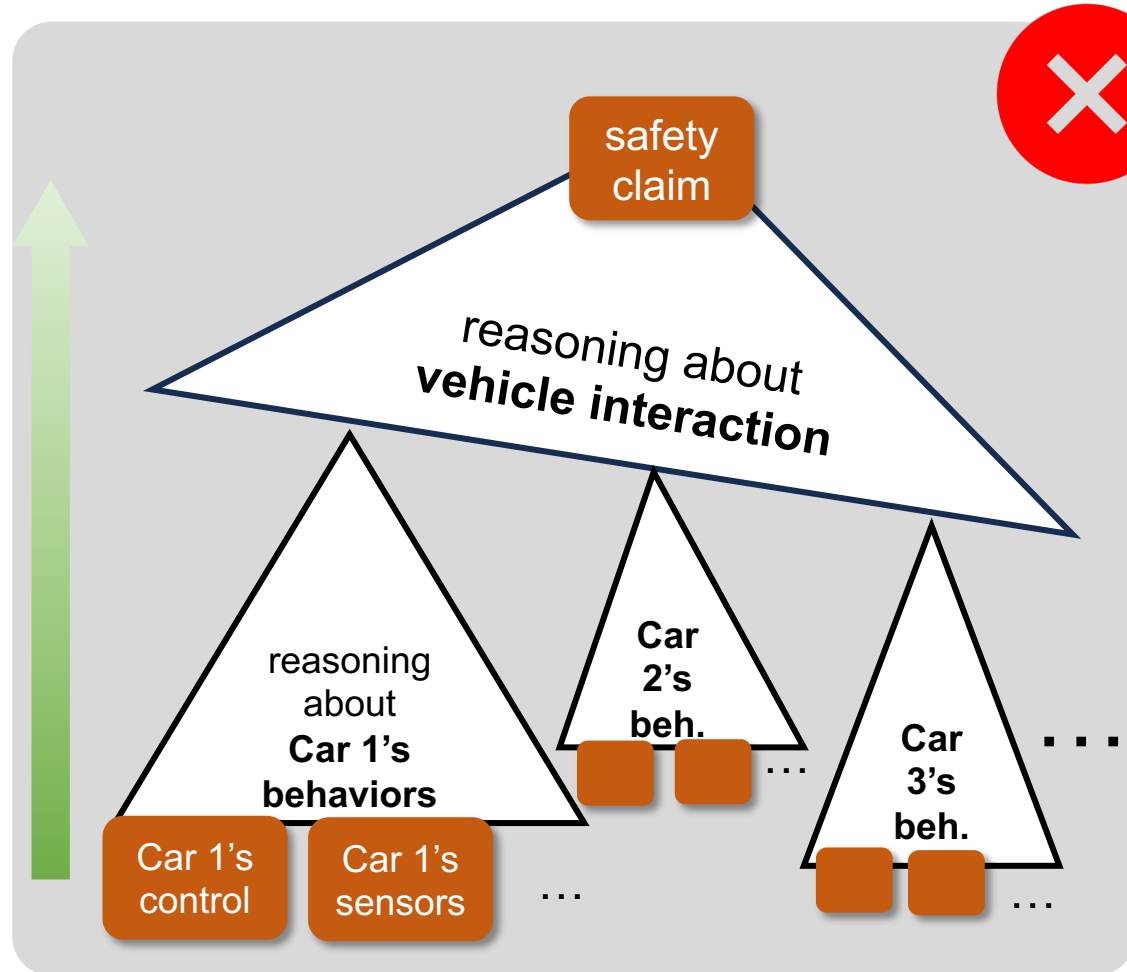


Mathematical safety proofs would certainly be great...

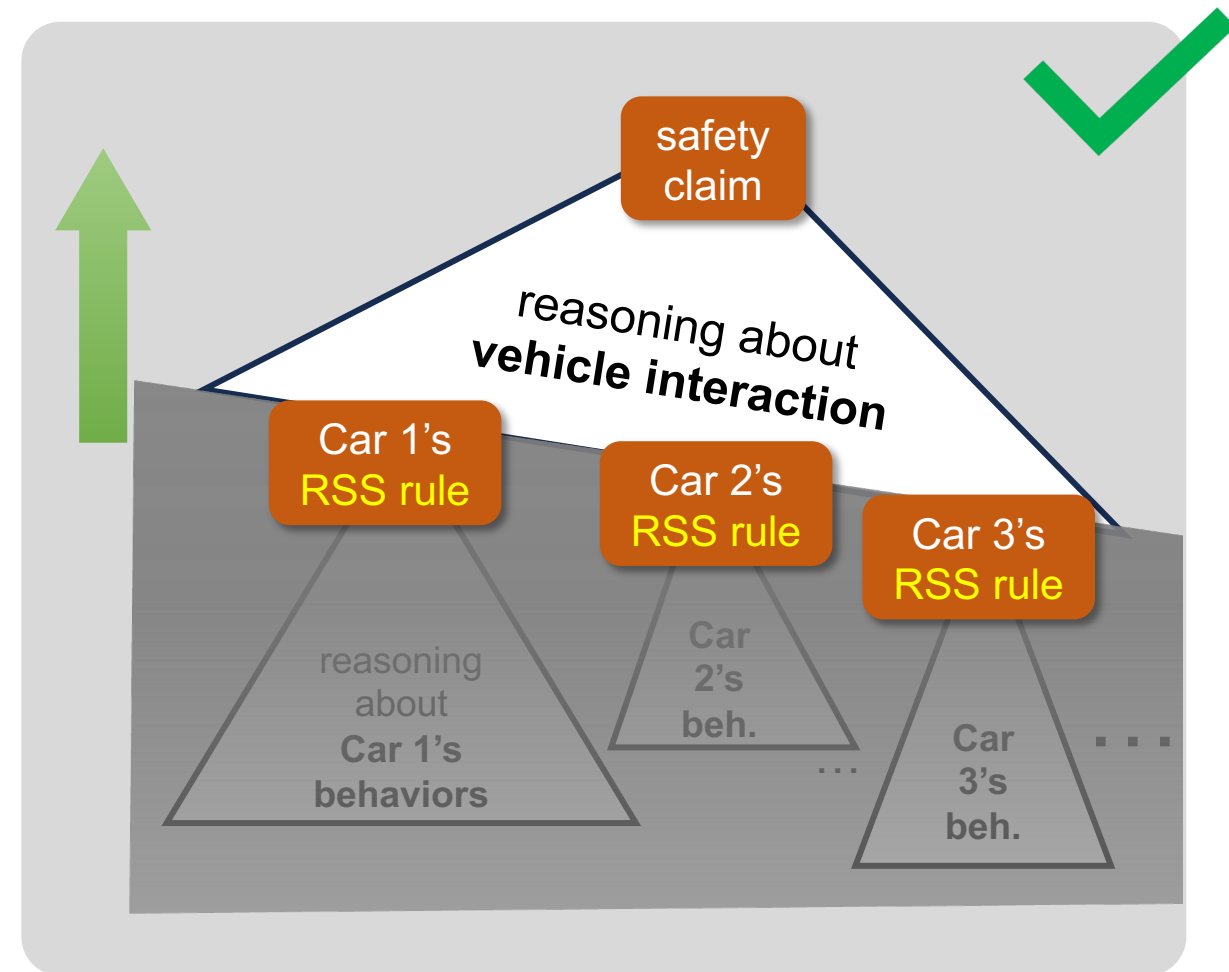
But are they ever feasible?

Responsibility-Sensitive Safety (RSS)

[Shalev-Shwartz et al., arXiv preprint, 2017]



- **Full safety proofs are infeasible**
 - Lack of white-box models
 - Ultimate safety claim is too far



- Ignore the internal working of individual vehicles
- Instead, impose “behavioral constructs” on them
 - Called **RSS rules**. “Mathematical traffic laws”
- Mathematical proofs assume rule compliance → feasible 31

RSS Rule, an Example

[Shalev-Shwartz et al., arXiv preprint, 2017]

- An RSS rule is a pair (A, α) of an *RSS condition* A and a *proper response* α



RSS condition A : (“You can still escape if A is true”)

Maintain an inter-vehicle distance at least

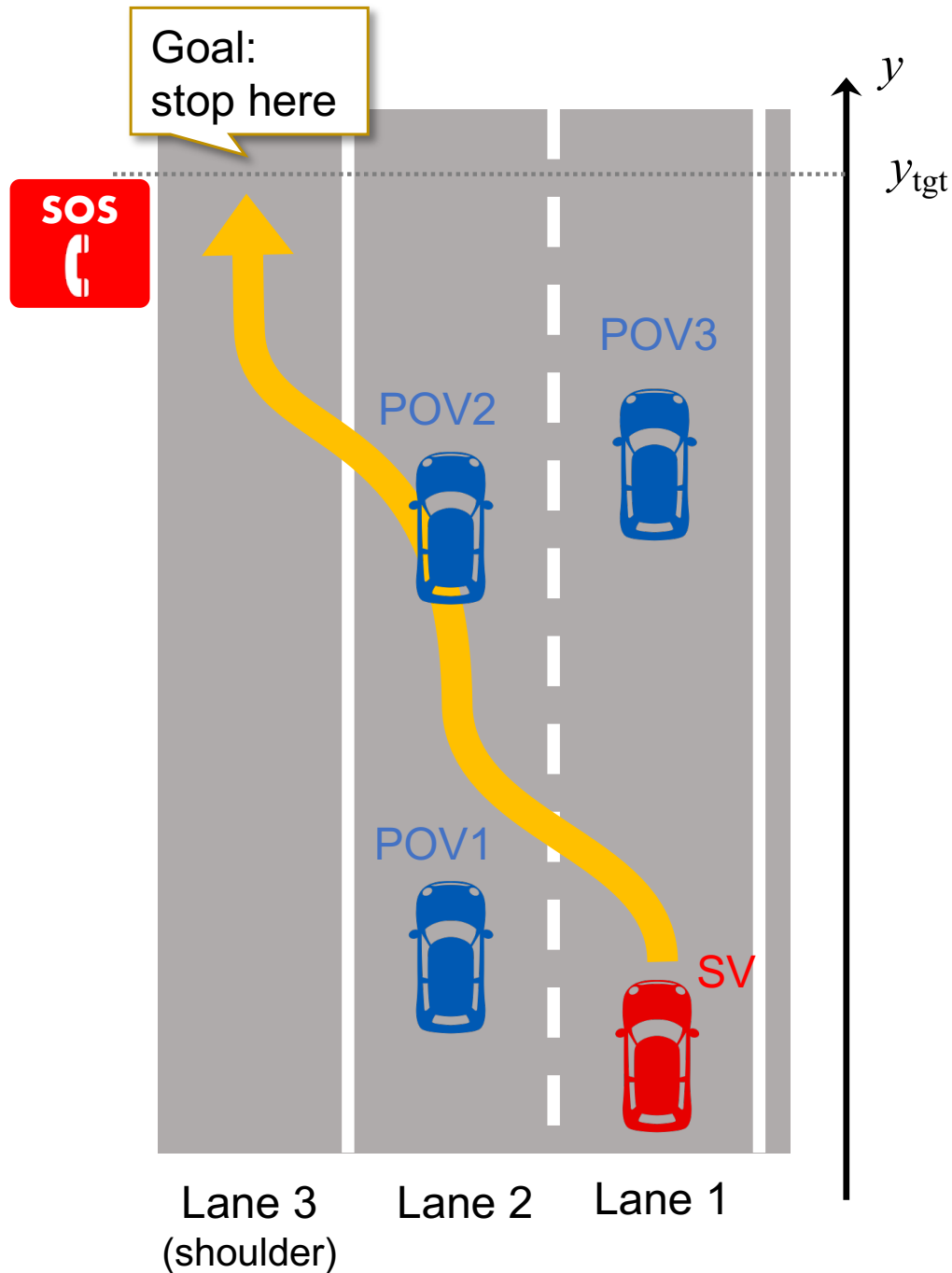
$$d_{\min} = \left[v_r \rho + \frac{1}{2} a_{\max, \text{accel}} \rho^2 + \frac{(v_r + \rho a_{\max, \text{accel}})^2}{2a_{\min, \text{brake}}} - \frac{v_f^2}{2a_{\max, \text{brake}}} \right]_+$$

Proper response α : (“When you escape, use the control strategy α ”)

Brake at rate $a_{\min, \text{brake}}$ within ρ seconds

Conditional safety lemma:

Any execution of α , from a state that satisfies A , is collision-free.



- Now what about this pull over scenario?
- Essential for eyes-off ADVs to hand the control over to human drivers
- Requires complex decision making
 - Merge before POV1, or after?
 - Accelerate to pass POV1...
 - ➔ Risk of overrun?



Our Work: Logical Formalization of RSS → More Scenarios (Collab. w/ Mazda)

RSS

Responsibility-Sensitive Safety, Shalev-Shwartz et al., 2017

- Basic methodology of logical safety rules
- Standardization (IEEE 2846)
- Lack of formal implementation → appl. to complex scenarios is hard
- Guarantees only collision-freedom so far

↓ Software science research

differential program logic dFHL (our contribution)

$$\begin{aligned} \text{inv: } & A \Rightarrow e_{\text{inv}} \sim 0 \quad e_{\text{var}} \geq 0 \wedge e_{\text{inv}} \sim 0 \Rightarrow \mathcal{L}\dot{x} = f \ e_{\text{inv}} \geq 0 \\ \text{var: } & A \Rightarrow e_{\text{var}} \geq 0 \quad e_{\text{var}} \geq 0 \wedge e_{\text{inv}} \sim 0 \Rightarrow \mathcal{L}\dot{x} = f \ e_{\text{var}} \leq e_{\text{ter}} \\ \text{ter: } & A \Rightarrow e_{\text{ter}} < 0 \quad e_{\text{var}} \geq 0 \wedge e_{\text{inv}} \sim 0 \Rightarrow \mathcal{L}\dot{x} = f \ e_{\text{ter}} \leq 0 \end{aligned}$$

$$\{A\} \text{dwhile}(e_{\text{var}} > 0) \dot{x} = f \{e_{\text{var}} = 0 \wedge e_{\text{inv}} \sim 0\} : e_{\text{inv}} \sim 0 \wedge e_{\text{var}} \geq 0 \quad (\text{DWH})$$

- A logical system for deriving and proving safety rules

Compositional rule derivation workflow by dFHL (our contribution)



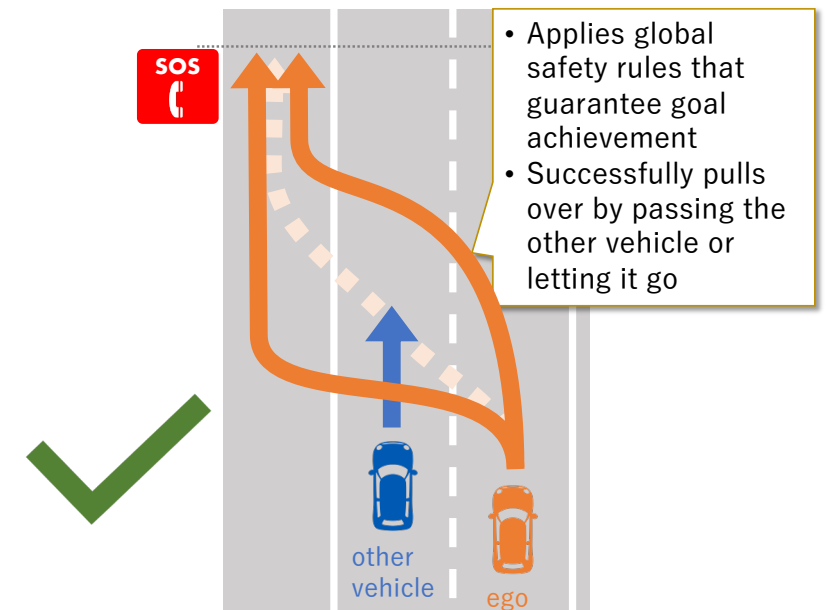
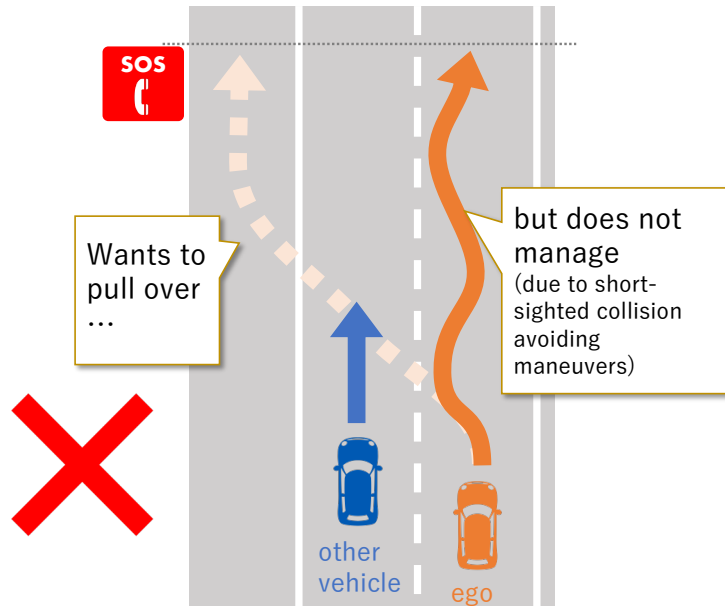
- "Divide and Conquer" complex driving scenarios
- Tool support by autom. reasoning

GA-RSS (our contribution)

Goal-Aware

Responsibility-Sensitive Safety [Hasuo+, IEEE T-IV, 2023]

- Guarantees goal achievement (e.g. successful pull over) and collision-freedom
- Global safety rules that combine mult. maneuvers
- Necessary for real-world complex driving scenarios



What is Formalization?

Informal pen-and-paper proofs



- Error-prone
- Poor traceability



Formal software-assisted proofs

A computer monitor displaying formal logical expressions and code. The screen shows several mathematical formulas and code snippets, including a figure caption and a final equality statement. The formulas involve variables like v , y , t , and θ , and operations like Integrate and Equal . The code snippets use a notation like $\text{In}(\cdot) :=$ and $\text{Out}(\cdot) :=$ to define variables and expressions.

Fig. 13: replacing not explicit presentc

- Symbolic proofs in our formal logical system dFHL
- Software tool checking the validity of each logical step of reasoning

RSS Rules as **Mathematical Traffic Laws**: Proof-Based Ecosystem for Safe Automated Driving



- Decompose safety (a complex goal) into logical safety rules (explicit, easy to check and enforce)
- “Ultimate assurance” in the form of mathematical proofs. Logical explanation by following their reasoning steps
- Safety rules are generic and reusable
→ regulation, standard → social acceptance
- Attribution of liabilities
(collision → someone must have broken the rules)

Safety Rule R_1

In the *same-lane same-direction* driving scenario,

- Maintain the safety distance

$$d_{\min} = \left[v_r \rho + \frac{1}{2} a_{\max, \text{accel}} \rho^2 + \frac{(v_r + \rho a_{\max, \text{accel}})^2}{2a_{\min, \text{brake}}} - \frac{v_f^2}{2a_{\max, \text{brake}}} \right]_+$$

from the preceding car

- When that’s hard, brake at acceleration $a_{\max, \text{brake}}$

Theorem (Safety)

There is no collision attributed to the ego vehicle as long as the safety rule R_1 is respected

Proof (of the safety thm.)

The only non-obvious point is that $e_{\text{inv},2}$ is preserved by the dynamics. We first observe

$$\mathcal{L}_{\delta_j, \delta_r} e_{\text{inv},2} = \begin{cases} 0 & \text{if } d\text{RSS}_{\pm}(v_f, v_r, \rho - t) \geq 0 \\ v_f - v_r & \text{otherwise,} \end{cases}$$

where $d\text{RSS}_{\pm}(v_f, v_r, \rho)$ is given by

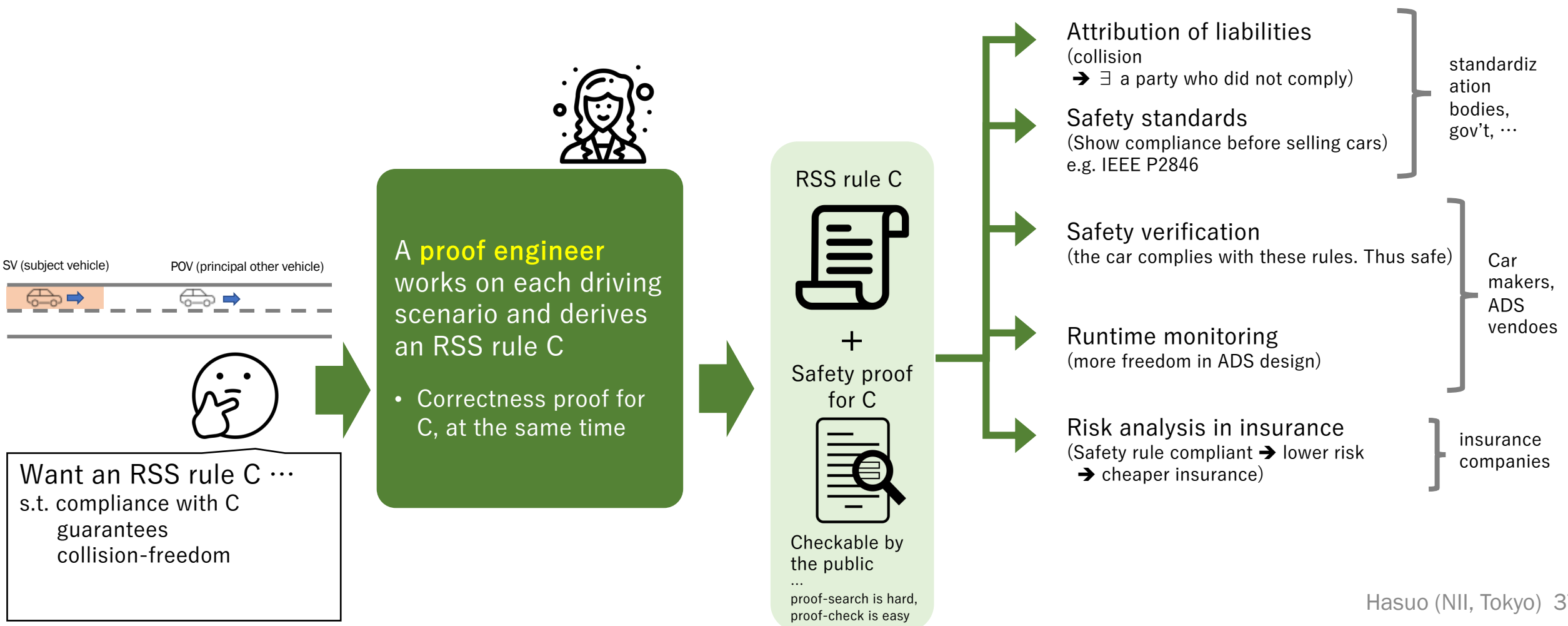
$$d\text{RSS}_{\pm}(v_f, v_r, \rho) = v_r \rho + \frac{a_{\max} \rho^2}{2} + \frac{(v_r + a_{\max} \rho)^2}{2b_{\min}} - \frac{v_f^2}{2b_{\max}}$$

Therefore, we can infer as follows.

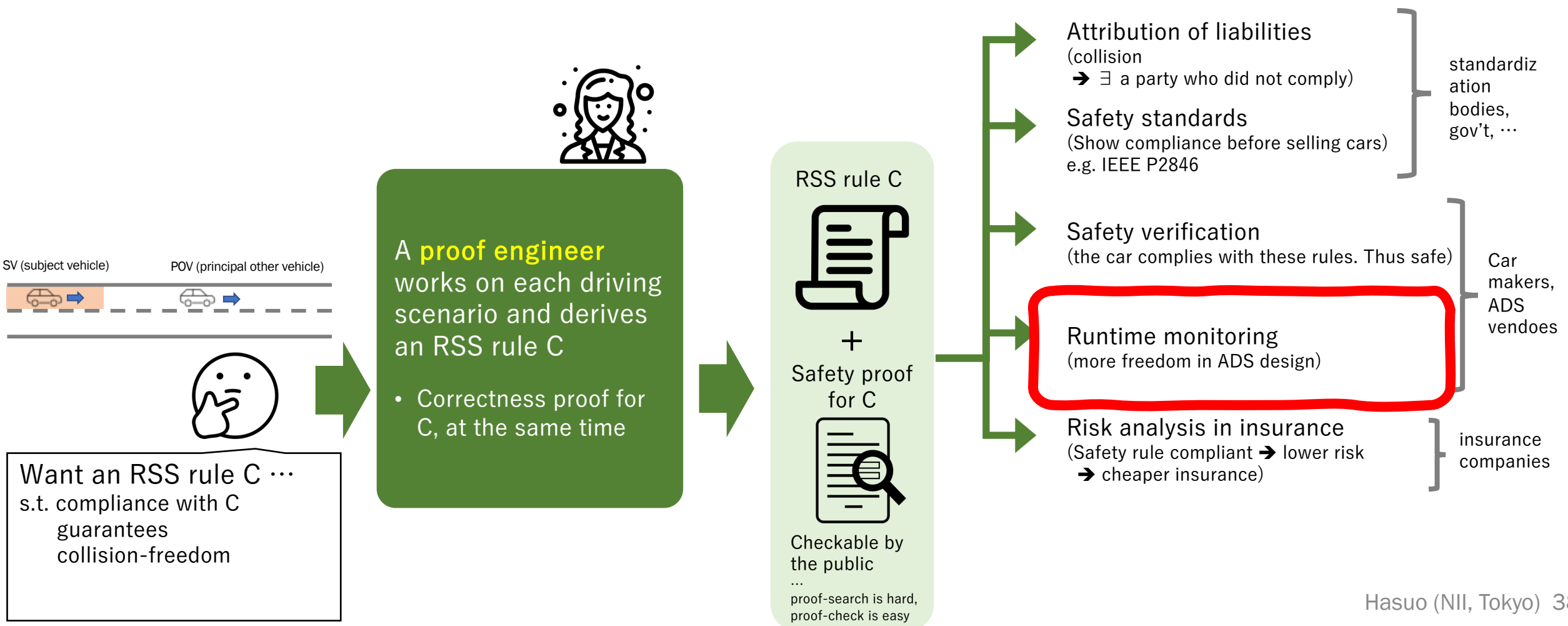
$$\begin{aligned} d\text{RSS}_{\pm}(v_f, v_r, \rho - t) &< 0 \\ \iff v_r(\rho - t) + \frac{a_{\max}(\rho - t)^2}{2} + \\ &\frac{(v_r + a_{\max}(\rho - t))^2}{2b_{\min}} - \frac{v_f^2}{2b_{\max}} < 0 \end{aligned}$$

R_1
 R_2
 R_3
...

RSS Rules as **Mathematical Traffic Laws**: Proof-Based Ecosystem for Safe Automated Driving



RSS Rules as **Mathematical Traffic Laws**: Proof-Based Ecosystem for Safe Automated Driving



Safety Envelope by RSS Rules

Can Be Retrofit to Any ADV Controller Monitor & Intervene → Runtime Safety Guarantee

RSS Rule, an Example

[Shalev-Shwartz et al., arXiv preprint, 2017]



- An RSS rule is a pair (A, α) of an **RSS condition** A and a **proper response** α

RSS condition A :

Maintain an inter-vehicle distance at least

$$d_{\min} = \left[v_r \rho + \frac{1}{2} a_{\max, \text{accel}} \rho^2 + \frac{(v_r + \rho a_{\max, \text{accel}})^2}{2a_{\min, \text{brake}}} - \frac{v_f^2}{2a_{\max, \text{brake}}} \right]_+$$

Proper response α :

If A is about to be violated, brake at rate $a_{\min, \text{brake}}$ within ρ seconds

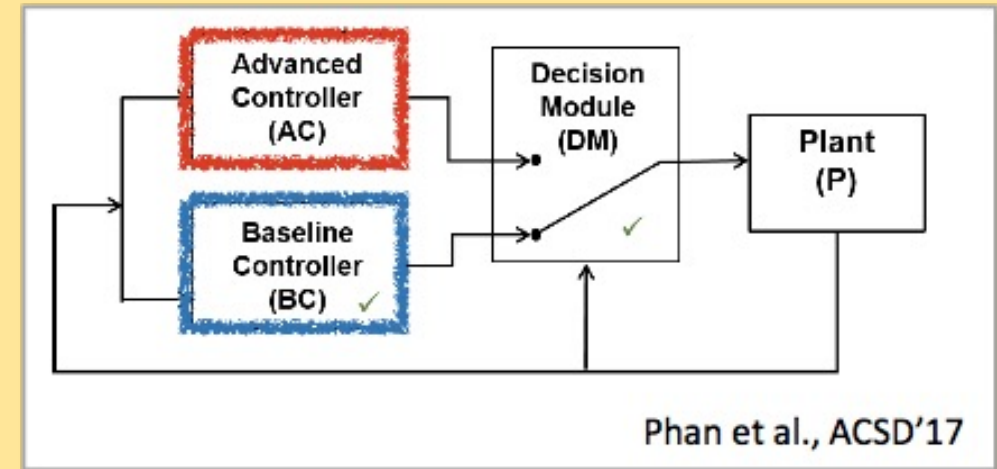
Conditional safety lemma:

Any execution of α , from a state that satisfies A , is collision-free.

Structure of an RSS rule

- RSS Condition A :
“You can still **escape** if A is true”
- Proper response α :
“control strategy to **escape**”

escape =
MRM
(minimum risk maneuver)

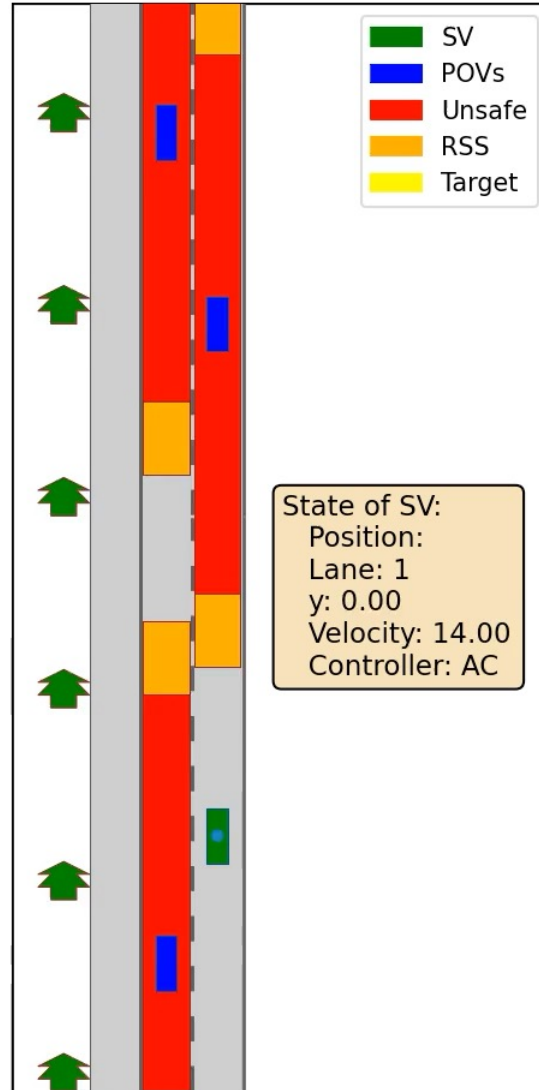


Simplex architecture

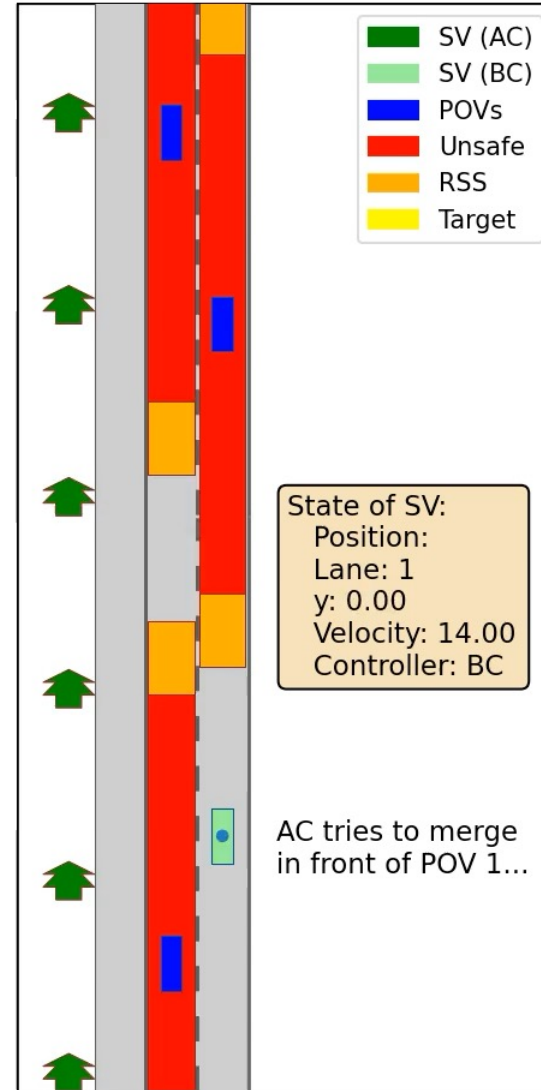
- AC pursues performance and safety
 - BC pursues safety (only)
 - DM (decision module) switches between them—
“use BC to escape”
- RSS rules fit perfectly!
- AC: existing controller (optimization-based, ML, ...)
 - BC: executes a proper response
 - DM: monitors an RSS condition. Violation foreseen → switch to BC

RSS Safety Envelopes in Action, Scenario I

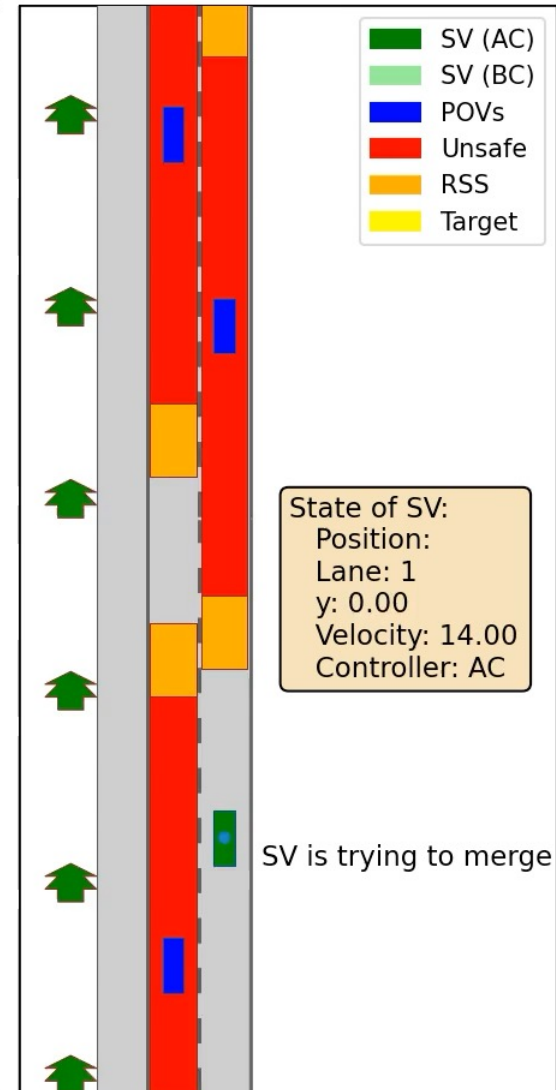
- **AC**: no safety envelope
 - **AC+RSS**:
Original RSS rule [Shalev-Shwartz et al., arXiv, 2017]
as a safety envelope
("short-sighted" collision avoidance)
 - **AC+RSS^{GA}**:
Our RSS rule [Hasuo+, IEEE T-IV]
as a safety envelope
(goal achievement too with longer-term
planning)
- **AC** is not safe (hazardous cut-in)
 - **AC+RSS** does not reach the shoulder
 - **AC+RSS^{GA}** successfully deployed the long term strategy of (brake → merge behind).
Achieved both safety and the goal



AC



AC+RSS



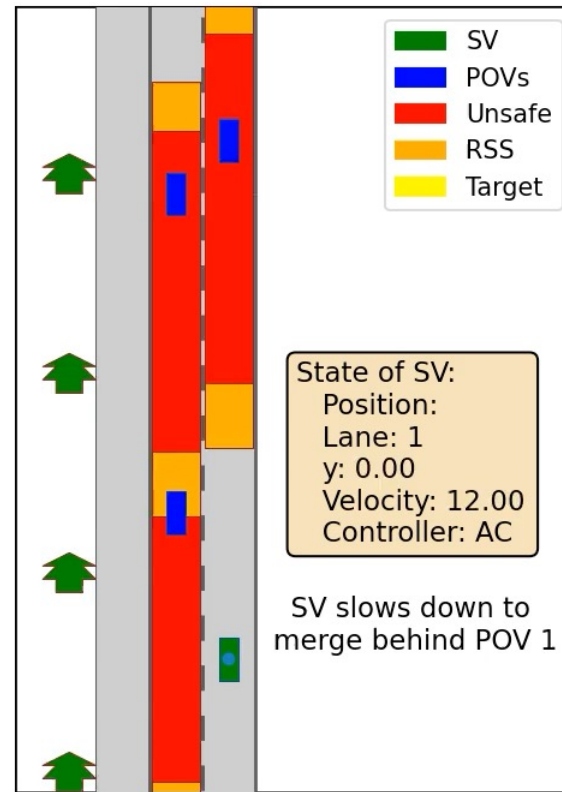
AC+RSS^{GA}

RSS Safety Envelopes in Action, Scenario II

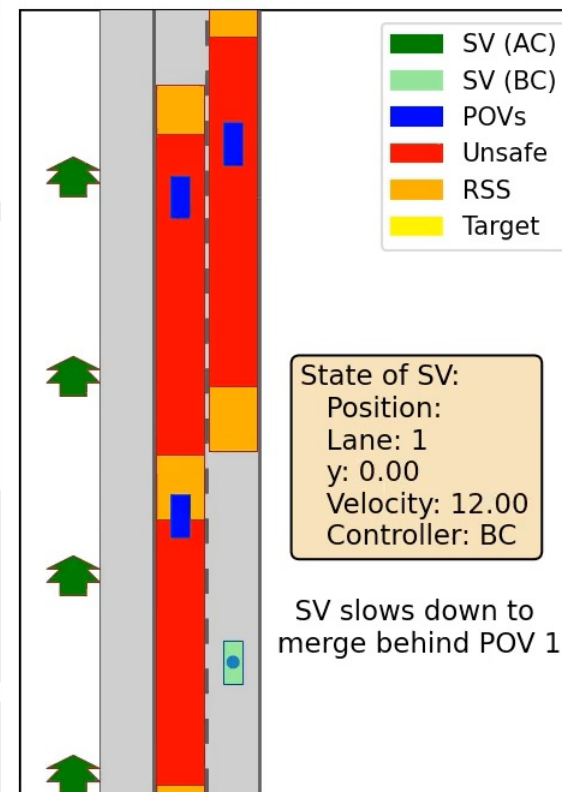
- **AC**: no safety envelope
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Original RSS rule
[Shalev-Shwartz et al., arXiv, 2017]
as a safety envelope
("short-sighted" collision avoidance)
- **AC+RSS^{GA}** :
Our RSS rule [Hasuo+, IEEE T-IV]
as a safety envelope
(goal achievement too
with longer-term planning)

- **AC** & **AC+RSS** safety achieve the goal, but are **slow**

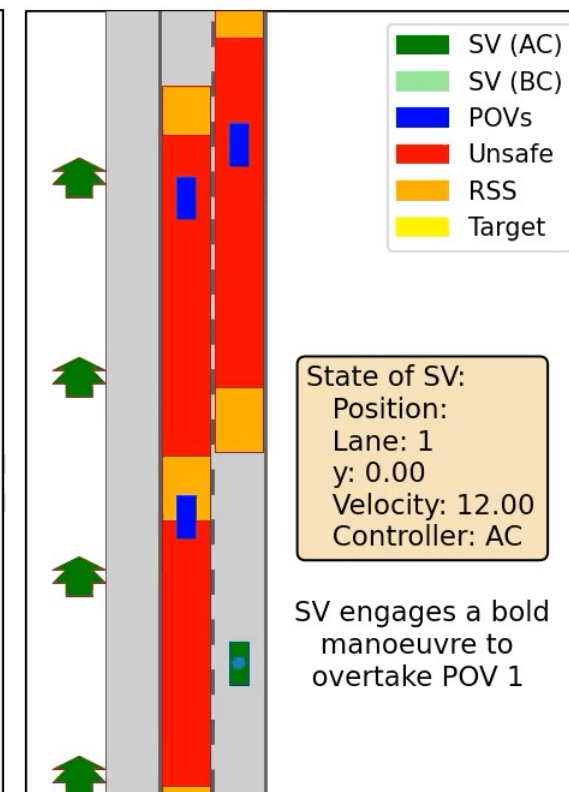
- **AC+RSS^{GA}**,
under mathematical safety guarantee,
boldly accelerates and merge in front



AC



AC+RSS



AC+RSS^{GA}

- ... who says safe ADVs are conservative and boring? 😊

DriveSSL – Our Live Demo (Under Devel.)

Tease an ADV... Can you cause an accident?



DriveSSL v2023.06.02
Safety & Goal Achievement via Logic

James Haydon, Benjamin R. Bray, Takashi Suwa, Ichiro Hasuo

Play + Step

Save Current State Restore Saved State Copy Saved JSON

Controller
Ours (Safeguard by Our Goal-Aware RSS)

Scenario
target position: 165

ego: brake [0-100] accel: 0
x: 8 y: 0 speed: 25

vehicle 3: brake [0-100] accel: 0
x: 8 y: 20 speed: 24

vehicle 2: brake [0-100] accel: 0
x: 4 y: 35 speed: 20

vehicle 1: brake [0-100] accel: 0
x: 4 y: 20 speed: 20

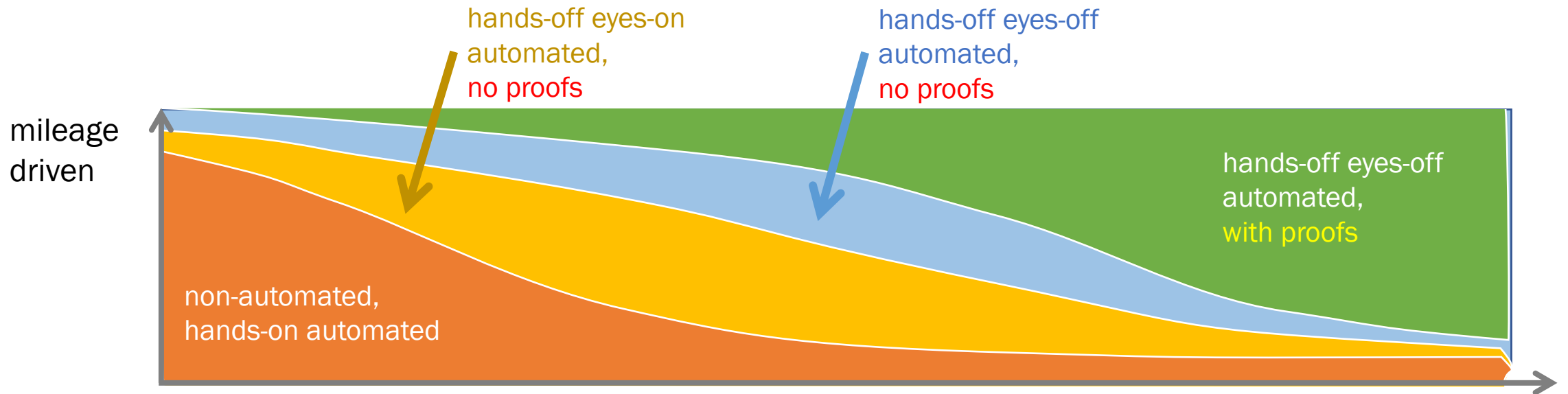
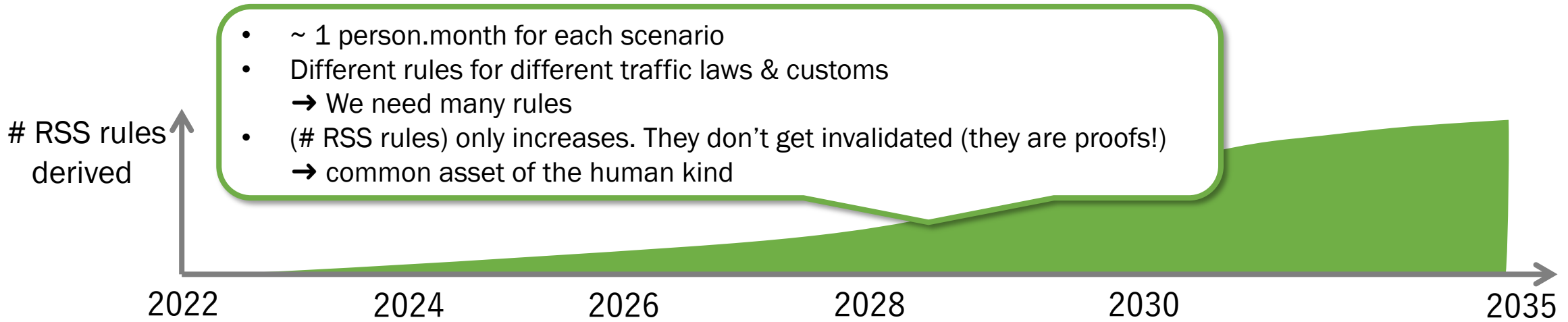
Scenarios Proper Responses Perf Stat Debug

1: Intermediate
3 lanes / 3 vehicles
Classic RSS guarantees collision avoidance, but...
No Safeguard: Merges too closely behind another vehicle, causing a safety violation.
Classic: Merges safely, guaranteeing collision avoidance.

2: Basic Safety Prevents Goal Achievement
3 lanes / 3 vehicles
Without a safeguard, a safety violation occurs. Classic RSS operates safely, but abandons the goal of merging.
No Safeguard: Causes a safety violation.
Classic: Operates safely, but overshoots the target because it cannot safely slow down fast enough.
Ours: Operates safely, while still reaching the target.

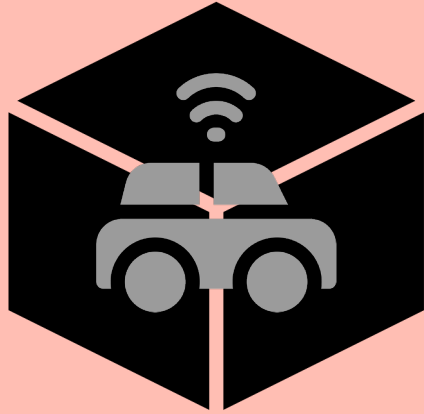
3: Daring, Yet Safety Guaranteed
3 lanes / 4 vehicles
Goal-Aware RSS can guarantee the safety of a risky-looking control.
No Safeguard: Waits for all other cars to pass before attempting to merge.
Classic: Waits for all other cars to pass before attempting to merge.
Ours: Accelerates to merge between vehicles in the neighboring lane.

Incremental Accumulation of RSS Rules, Incremental ODD Expansion of “ADVs with Proofs”



Two Possible Shapes of ADV Safety. Which is Better?

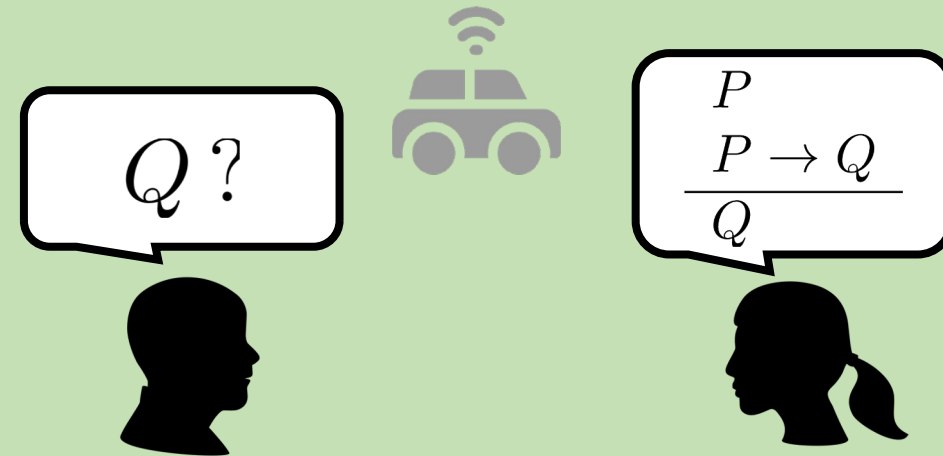
Blackbox Safety



- Monolithic “safety claims”
- Hard to examine, criticize, or improve

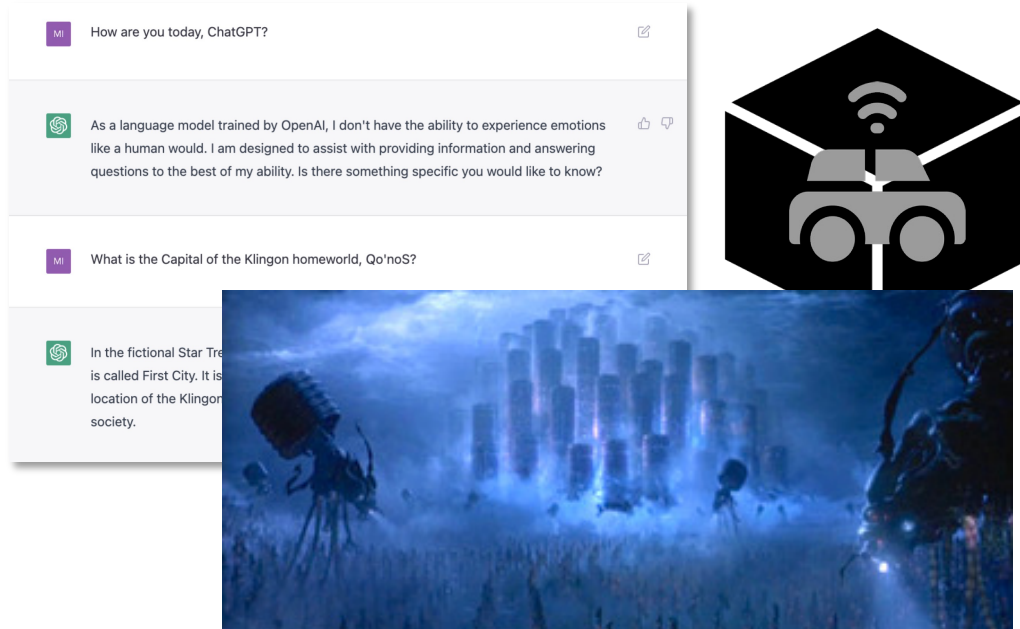
vs

Accountable Safety

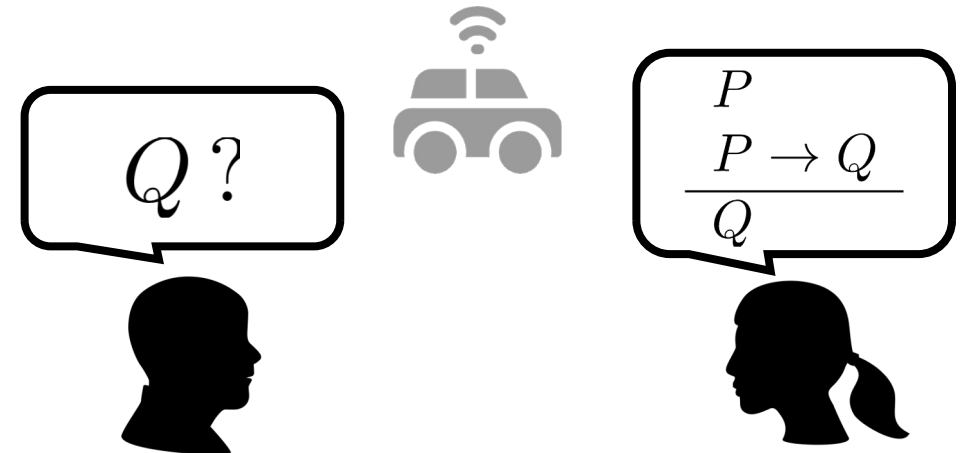


- Explainable and traceable safety cases structured by **logic**
- Supporting society’s collective and endless efforts towards ADV safety
- **The shape that we pursue**

Safety-Critical Systems Should Never be Blackbox Proofs Explicate Assumptions, Contracts, ODDs, and Responsibilities



- Many emerging technologies are statistical and blackbox
- We shouldn't let them operate in safety-critical domains
- (... fight against the “lawyer up” approach towards safety!)



- Conventionally:
Proofs are for establishing absolute truths
- New: proofs are **communication media** for
 - explicating assumptions and contracts,
 - showing who's responsible for what, and
 - writing and assessing safety cases
- Logiic as a social infrastructure for trust in ICT

Summary: Logical Manifestation of Specifications, Requirements and Responsibilities

Part 1

Formal methods for (conventional) software

(e.g. model checking)

Goal:

to *prove* $\mathcal{M} \models \varphi$

- “A system \mathcal{M} satisfies a req./spec./property φ ”
- Conventionally: \mathcal{M} is a program
 φ is “bug-free”
→ *bug-free proofs*

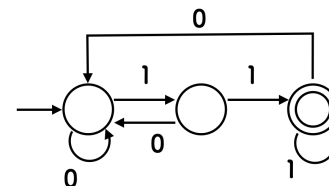
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Heavy-weight formal methods for manufacturing

Goal:

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- \mathcal{M} is a car
 φ is safety/quality/...
- But **we need a mathematical/logical model \mathcal{M} of a car!**



Modeling is costly

- MBD usually doesn't help
- Simulink is for numeric simulation, not principally for logical verification

Light-weight formal methods

→ *Manufacturing DX*

- Formal/math./software description of φ
- Feasible yet powerful

Part 2

Proof-based

mathematical traffic laws
for automated driving

- For int'l safety standards, a sound ecosystem, & social acceptance